

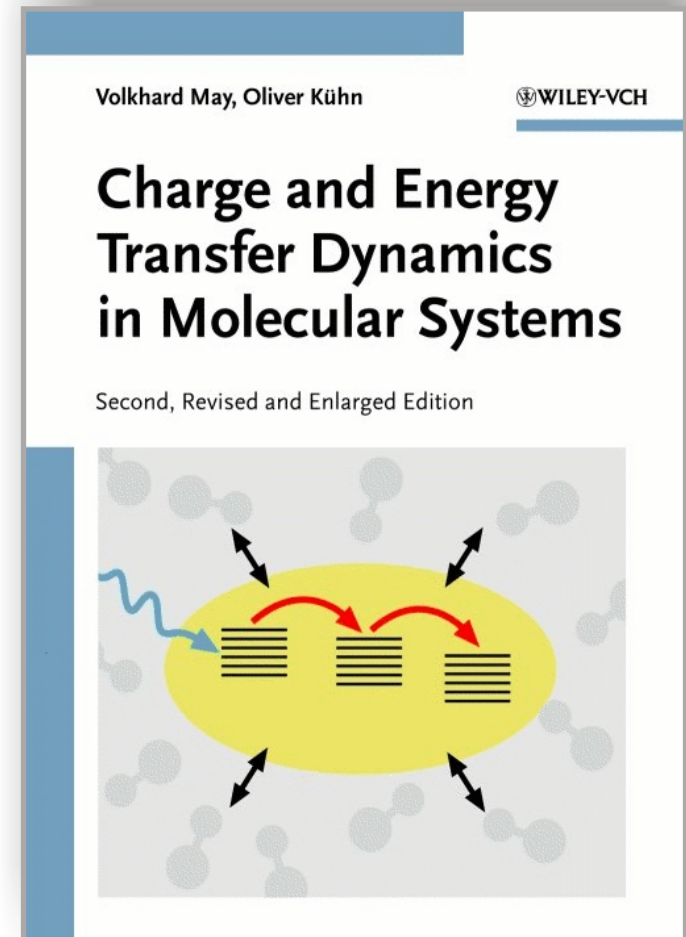
# Ultrafast Transfer Processes in Molecular Nanostructures



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Humboldt-University at Berlin

Chemical Physics  
Physical Chemistry  
Spectroscopy  
Nanotechnology

Quantum Dynamics of  
Molecular Systems







# Quantum Transport in Molecular Systems

## Theory

- photoinduced quantum dynamics in closed and open systems
- wave packet dynamics
- density matrix theory
- computation of optical signals
- mixed quantum-classical description
- electron structure calculations
- MD simulations

## Experiment

- relation of transient optical and infrared signals to molecular dynamics
- laser pulse control of molecular dynamics

# Systems and Processes to be Discussed

## introductory examples

- electron transfer in donor-acceptor systems
- charge transfer through single molecules
- dynamics of Frenkel excitons
- laser pulse control

## laser pulse control of non-adiabatic transitions

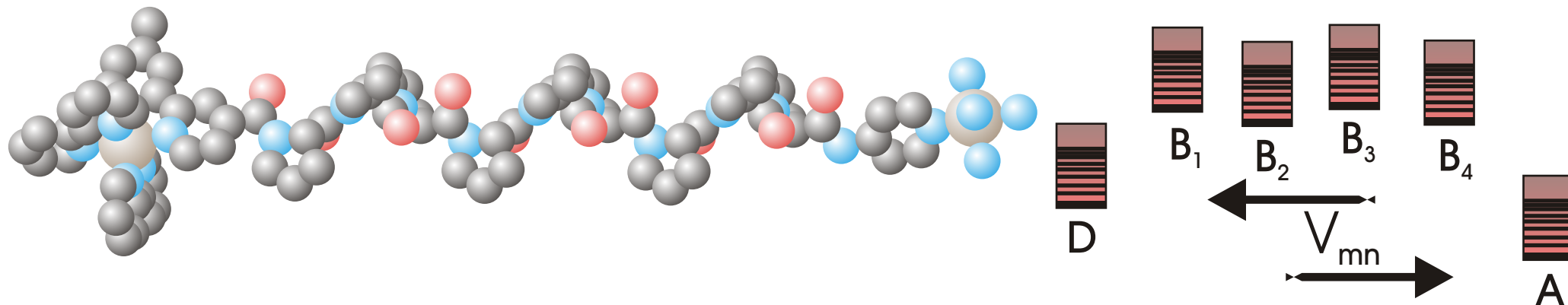
## heterogeneous electron transfer

## excitation energy transfer in supramolecular complexes

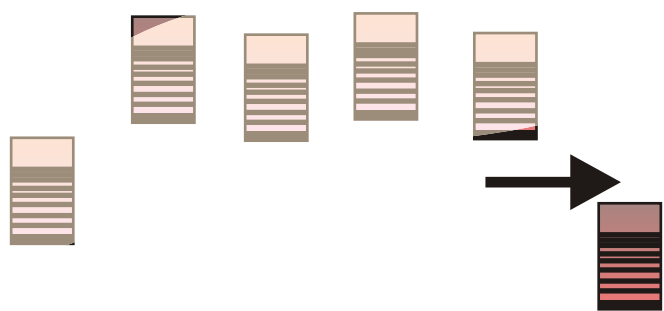


# Introductory Examples

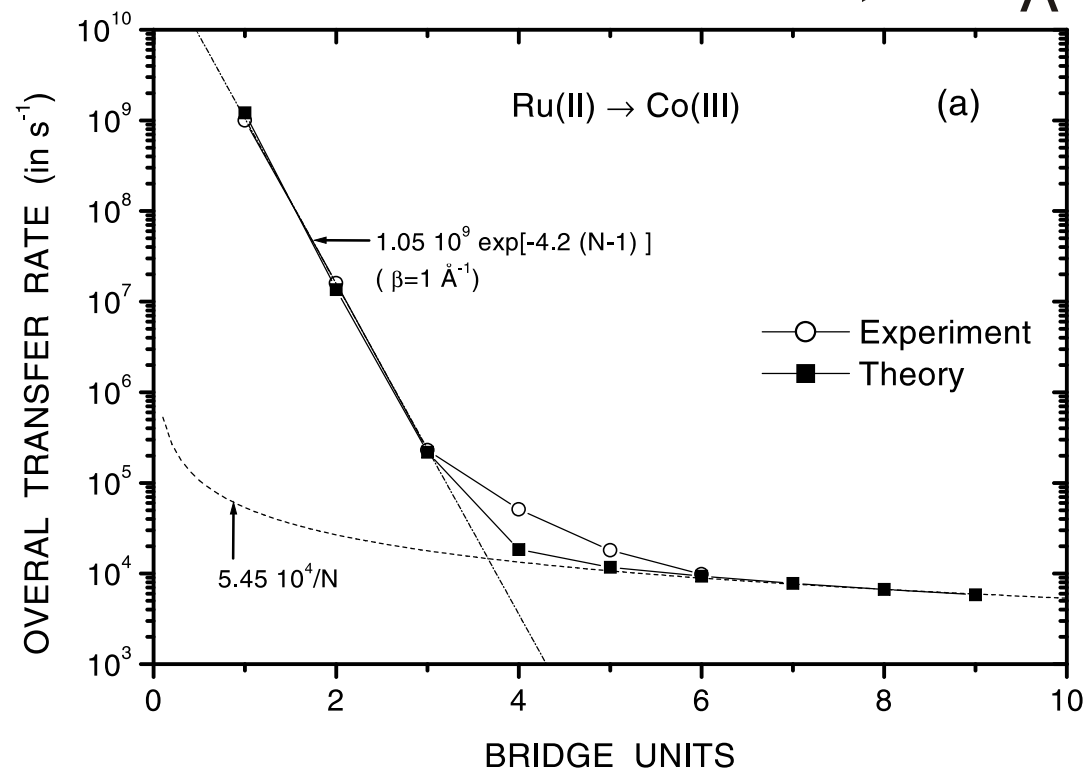
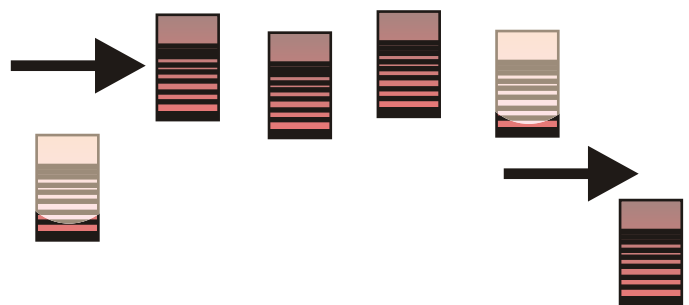
# Polyproline Mediated Electron Transfer



Superexchange ET

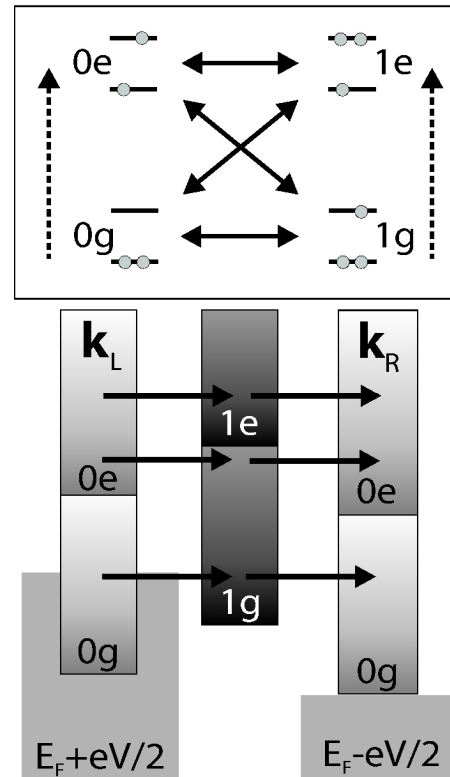
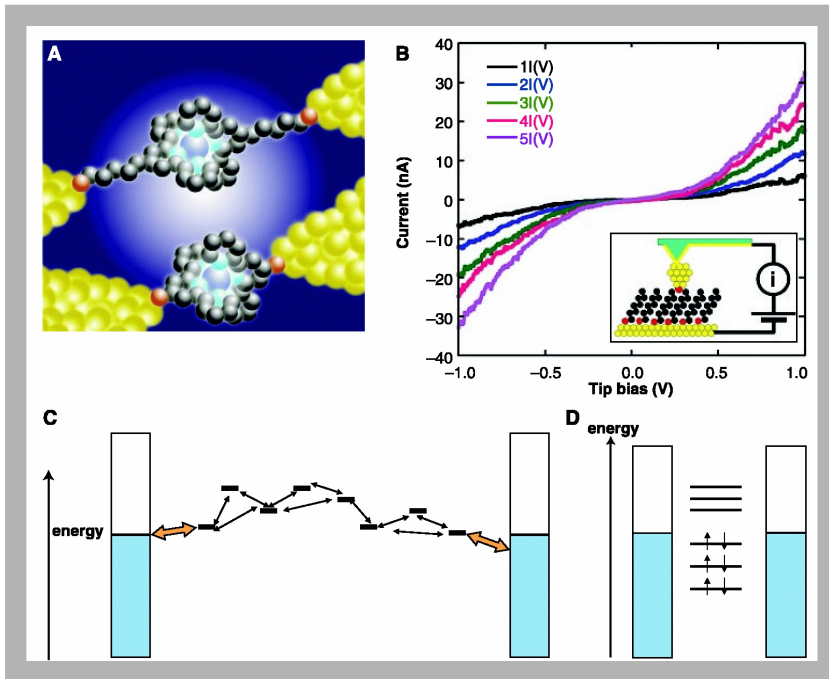


Sequential ET

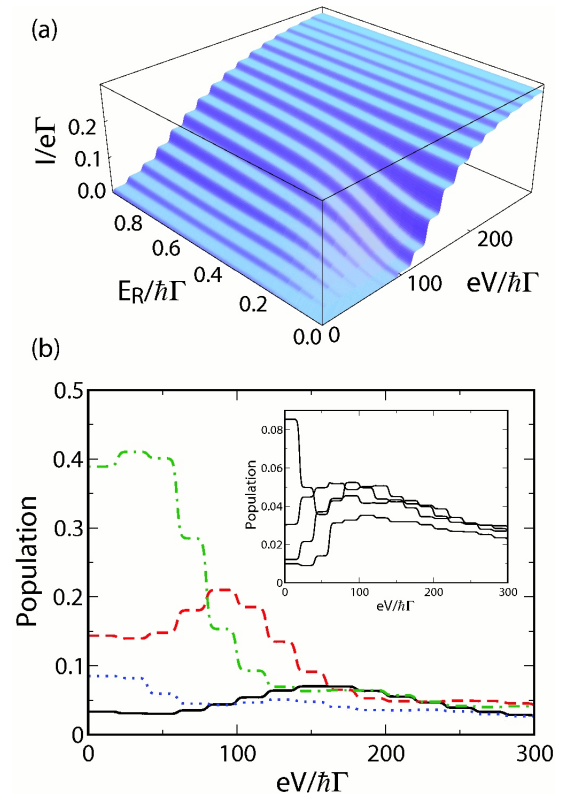


E.G. Petrov and V. May, J. Phys. Chem. A 105, 10176 (2001)

# Current through Single Molecules



Schematic view of possible charge transfer (solid arrows) and photoinduced (dashed arrows) transitions.



(a) Total current versus applied voltage and external field--strength  
(b) Stationary vibrational populations in the electronic ground state of the neutral molecule

V. May and O. Kühn:  
Photoinduced Removal of the  
Franck-Condon Blockade in Single  
Electron Inelastic Charge Transmission  
Nano Lett. 8, 1095 (2008).



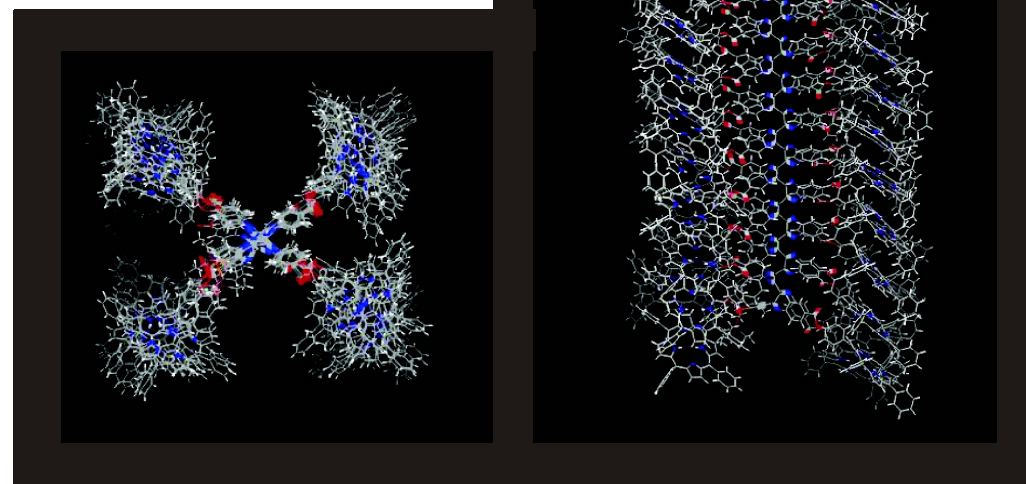
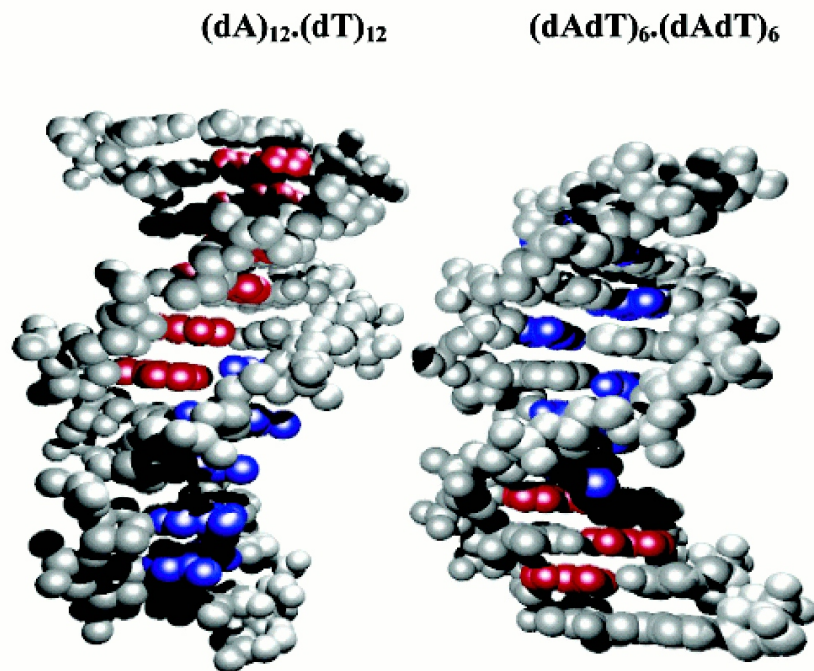
# Frenkel Excitons in Molecular Systems

## excitons in DNA

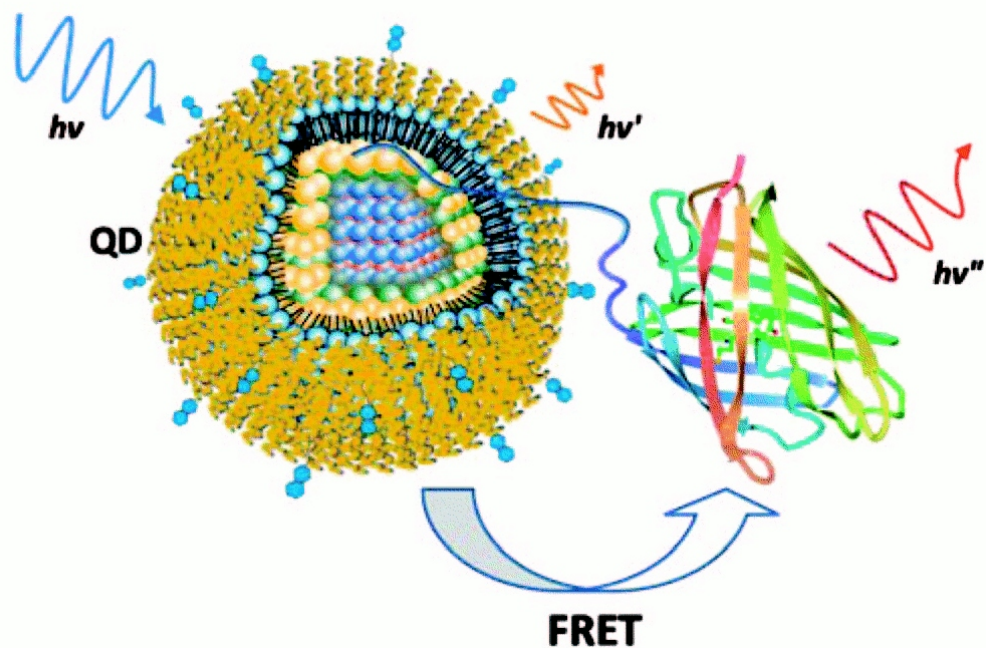
E. Emanuele, K. Zakrzewska, D. Markovitsi, R. Lavery, and P. Millie, *J. Phys. Chem. B* 109, 16109 (2005).

## excitation energy transfer in complex artificial structures

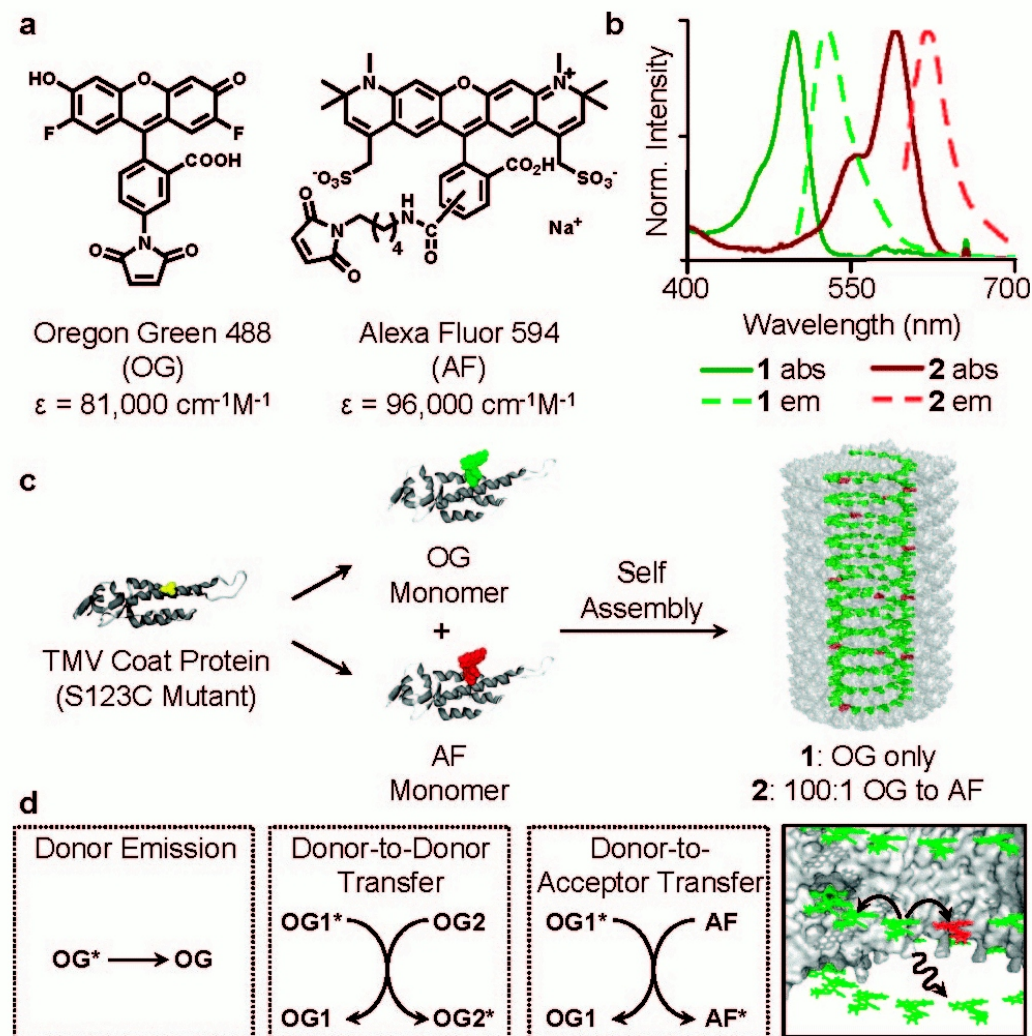
H. Zhu, M. Fujitsuka, A. Okada, S. Tojo, F. Takei, K. Onitsuka, S. Takahashi, and T. Majima, **Rapid Exciton Migration and Fluorescent Energy Transfer in Helical Polyisocyanides with Regularly Arranged Porphyrin Pendants**, *J. Phys. Chem. B* 108, 11935 (2004).



Y.-Z. Ma, R. A. Miller, G. R. Fleming, and M. B. Francis,  
**Energy Transfer Dynamics in Light-Harvesting Assemblies  
 Templated by Tobacco Mosaic Virus Coat Protein,**  
 J. Phys. Chem. B 112, 6887 (2008).



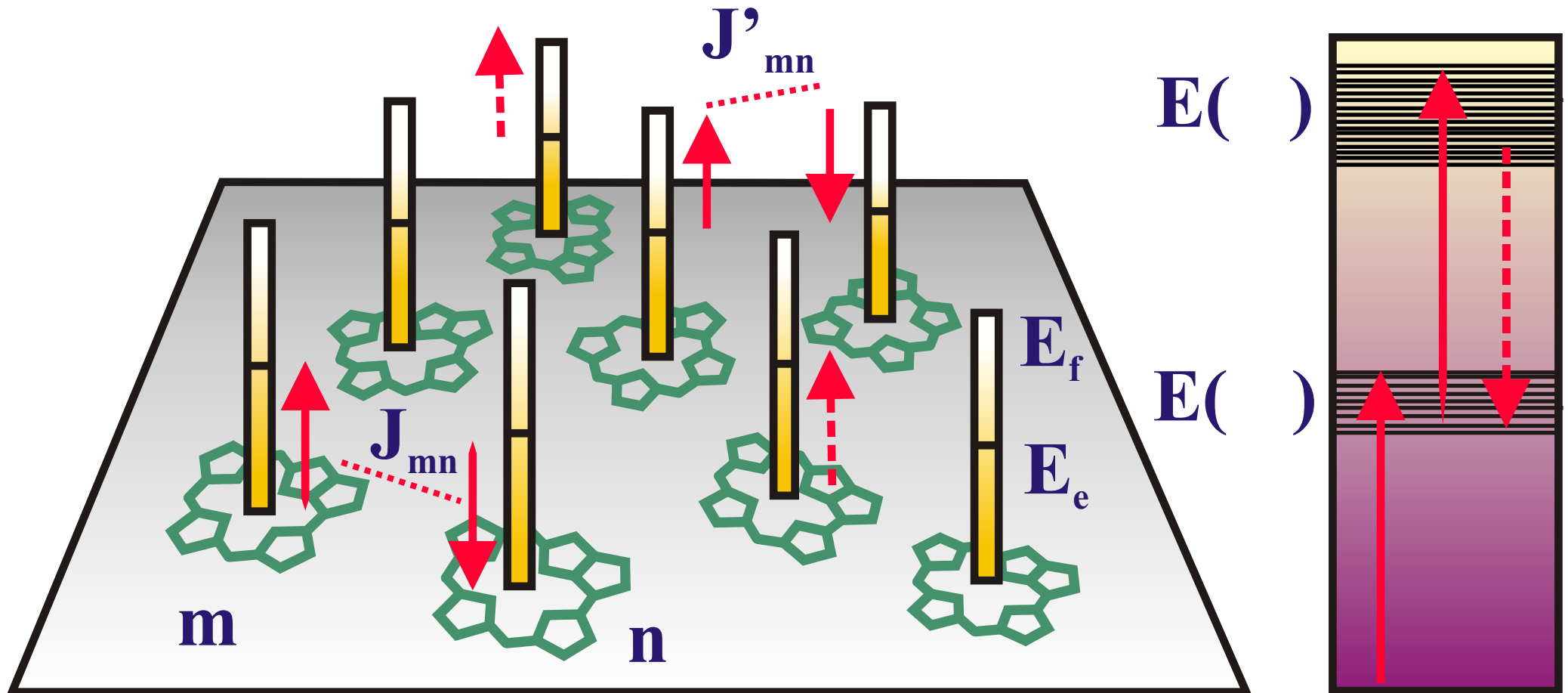
A. M. Dennis and G. Bao, **Quantum  
 Dot-Fluorescent Protein Pairs as Novel  
 Fluorescence Resonance Energy  
 Transfer Probes,**  
 NanoLett. 8, 1439 (2008).



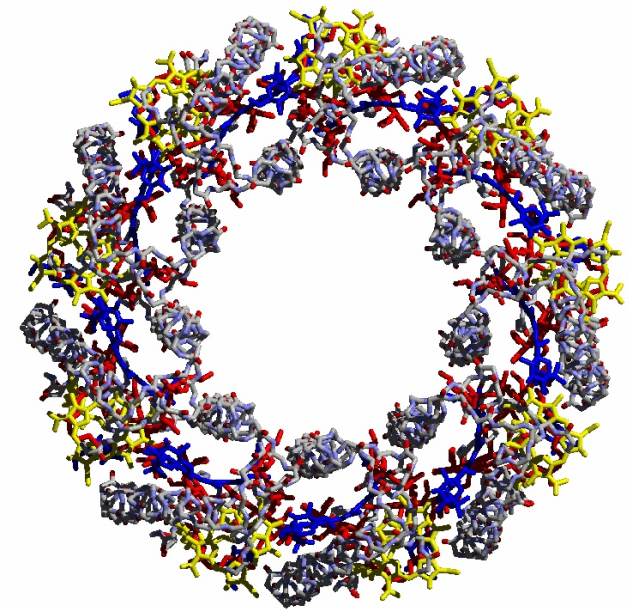
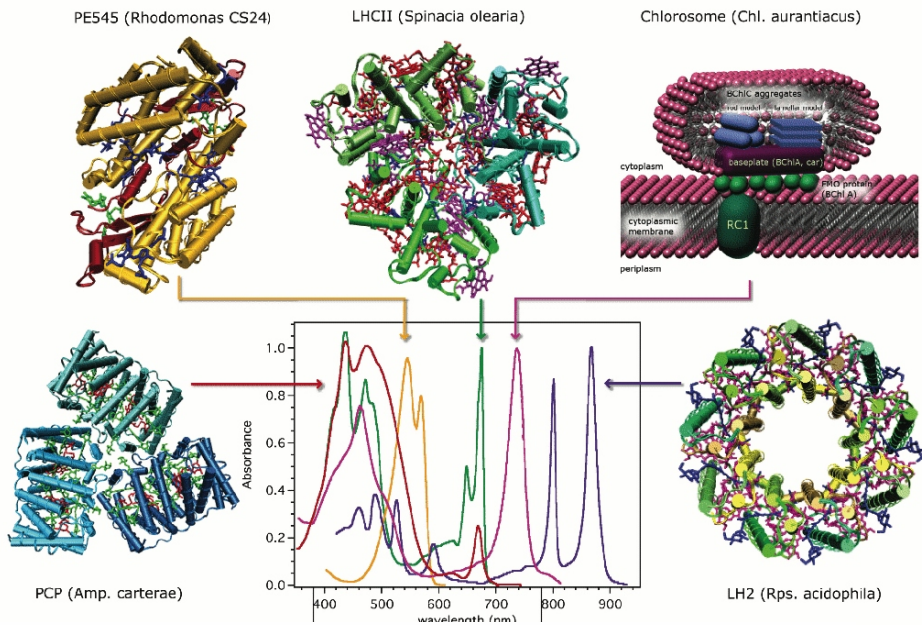
# The Standard Frenkel-Exciton Model

delocalized state  
representation

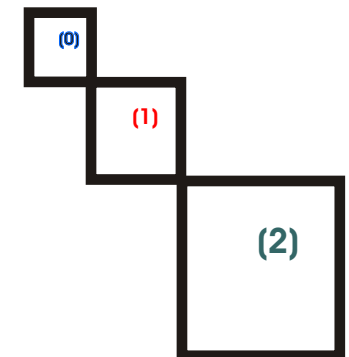
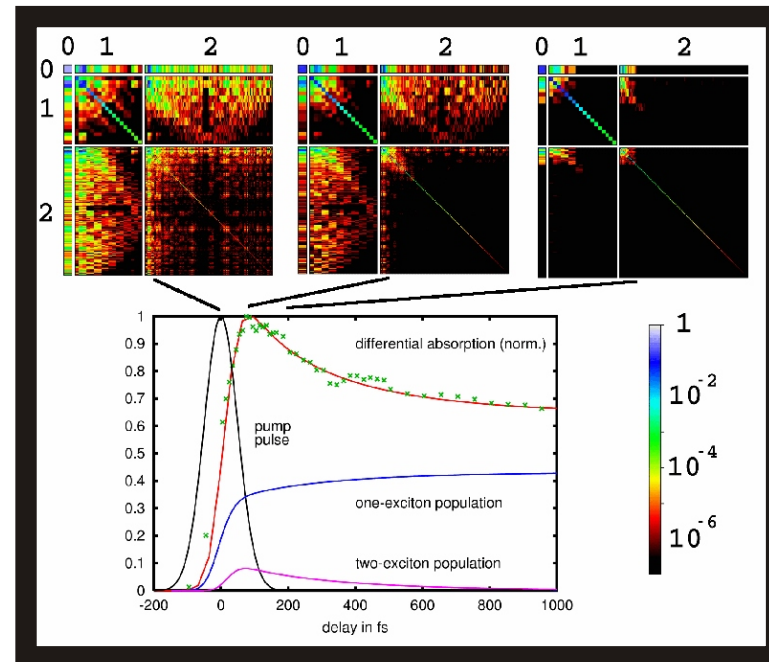
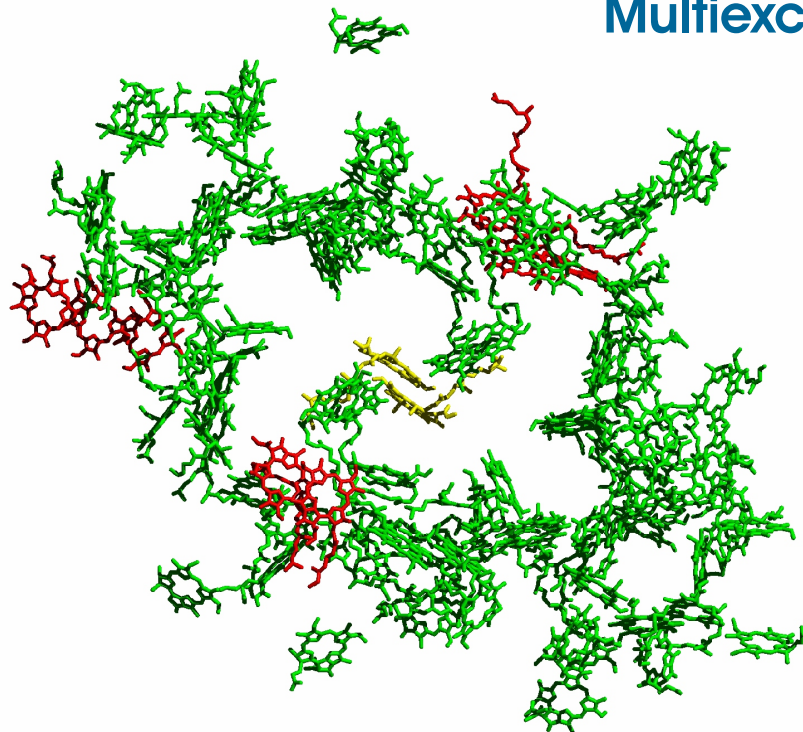
localized state representation







## Multiexciton Dynamics and Transient Absorption of the LH2



B. Brüggemann  
and V. M., JCP 120,  
2325 (2004)

# Condensed Phase Molecular Dynamics

## Electron Nuclei Dynamics in Molecular Systems

molecular Hamiltonian  $H_{\text{mol}} = T_{\text{nuc}} + H_{\text{el}}(R)$

adiabatic electronic states  $H_{\text{el}}(R)\varphi_a(r; R) = U_a(R)\varphi_a(r; R)$

expansion of the molecular wave function  $\Psi(r, R; t) = \sum_a \chi_a(R, t)\varphi_a(r; R)$

time-dependent Schrödinger equation of the nuclear motion

$$i\hbar \frac{\partial}{\partial t} \chi_a(R, t) = (T_{\text{nuc}} + U_a(R))\chi_a(R, t) + \sum_b \hat{\Theta}_{ab} \chi_b(R, t)$$

problems:

- > huge number of coordinates
- > study of thermal ensembles
- > coupling to a solvent or other types of condensed phase environment

## reduced quantum dynamics

reduced density operator

$$\hat{\rho}(t) = \int dR \langle R | \hat{W}(t) | R \rangle \equiv \text{tr}_{\text{nuc}} \{ \hat{W}(t) \}$$

electronic density matrix  $\rightarrow$  density matrix equations

$$\rho_{ab}(t) = \langle \varphi_a | \hat{\rho}(t) | \varphi_b \rangle$$

state population  $\rightarrow$  master equations

$$P_a(t) = \rho_{aa}(t)$$

## mixed quantum classical dynamics

quantum mechanical description of the electrons  $\rightarrow \varphi_a(r; R)$

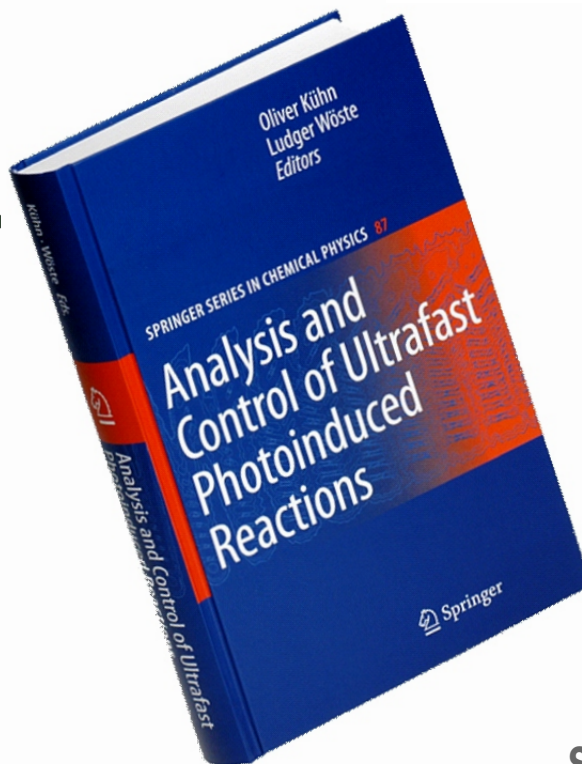
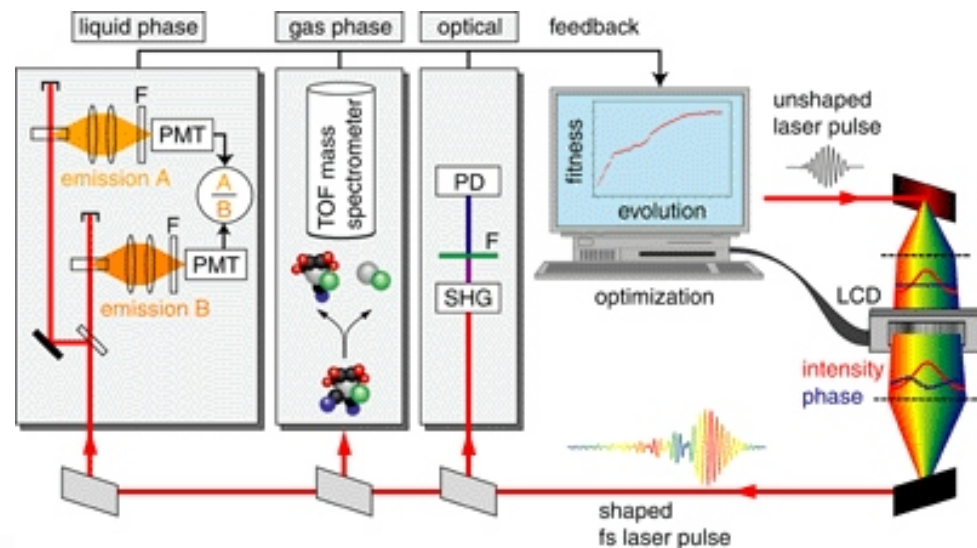
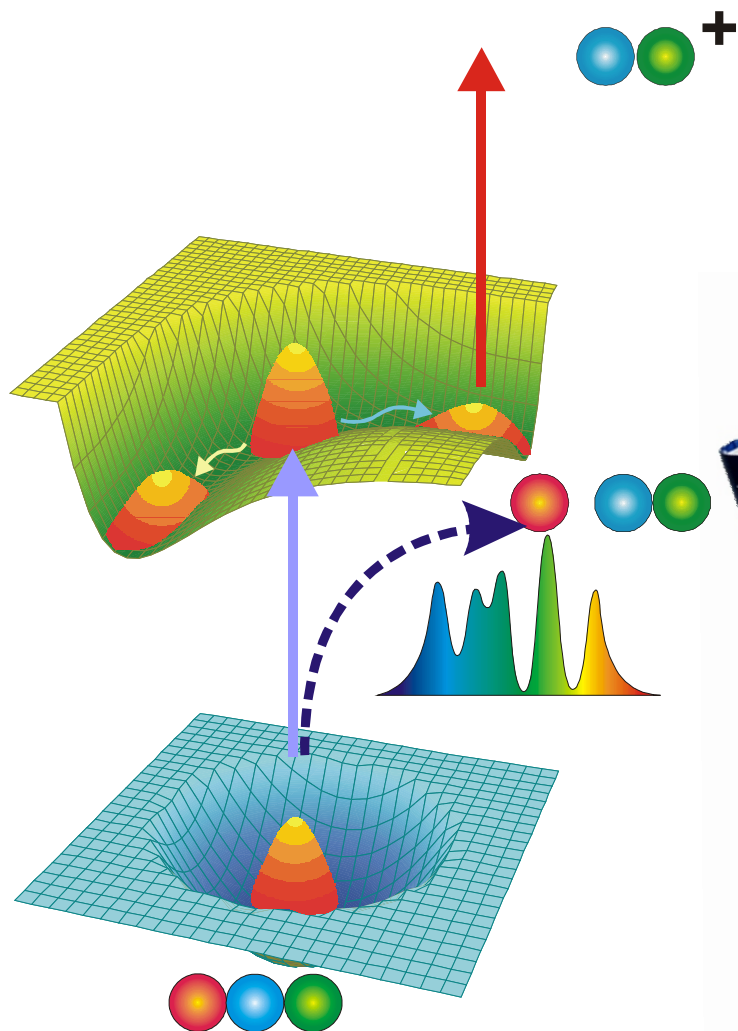
classical description of the nuclei  $\rightarrow R(t)$

$$i\hbar \frac{\partial}{\partial t} \phi(r, R(t); t) = H_{\text{el}}(R(t)) \phi(r, R(t); t)$$

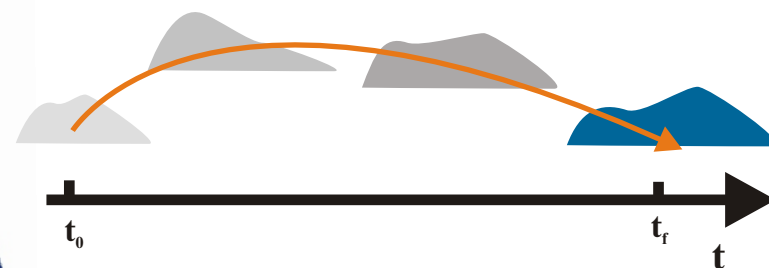
$$M_\nu \frac{\partial^2}{\partial t^2} \mathbf{R}_\nu(t) = -\nabla \langle \phi(R(t); t) | H_{\text{el}} | \phi(R(t); t) \rangle$$



# Laser Pulse Control of Molecular Dynamics



## Adaptive Femtosecond Quantum Control



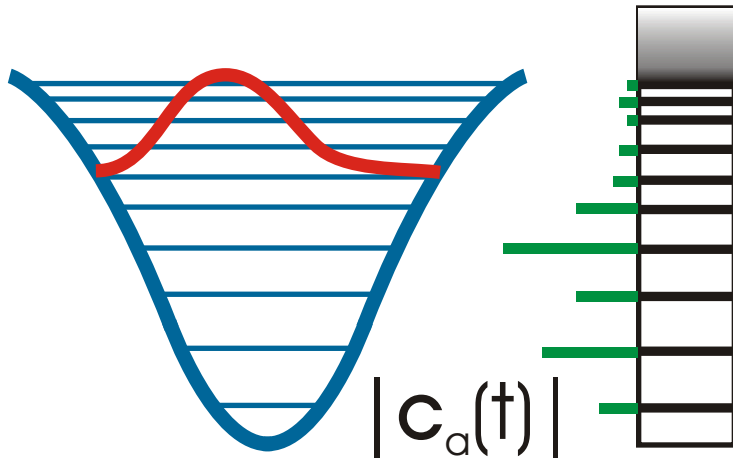
"Analysis and Control of Ultrafast Photoinduced Reactions"

O. Kühn and L. Wöste (eds.)

Springer Series in Chemical Physics,  
Vol. 87 (Springer-Verlag, 2007)

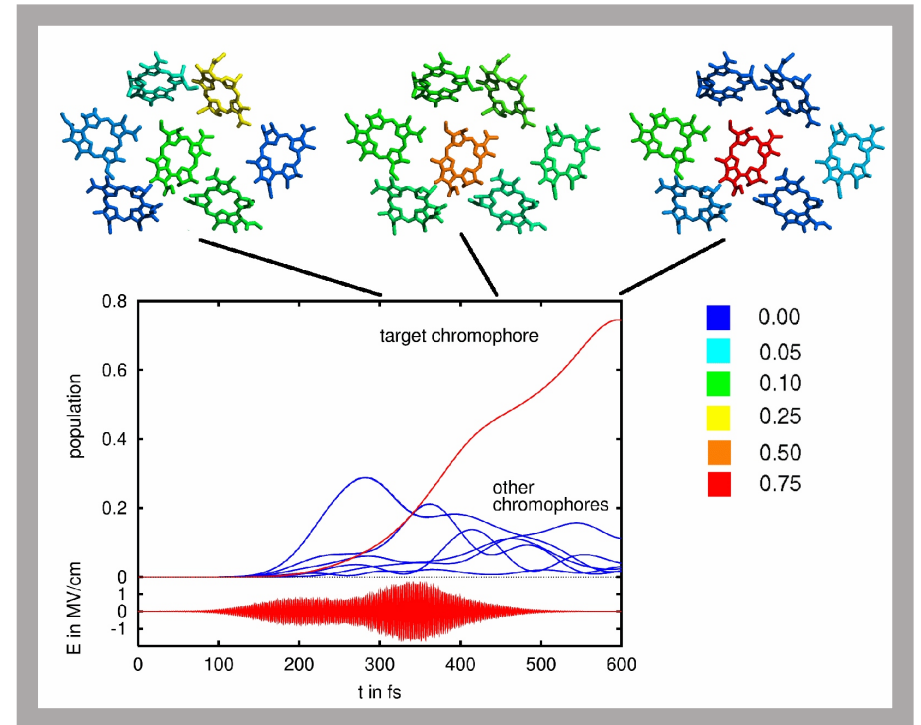
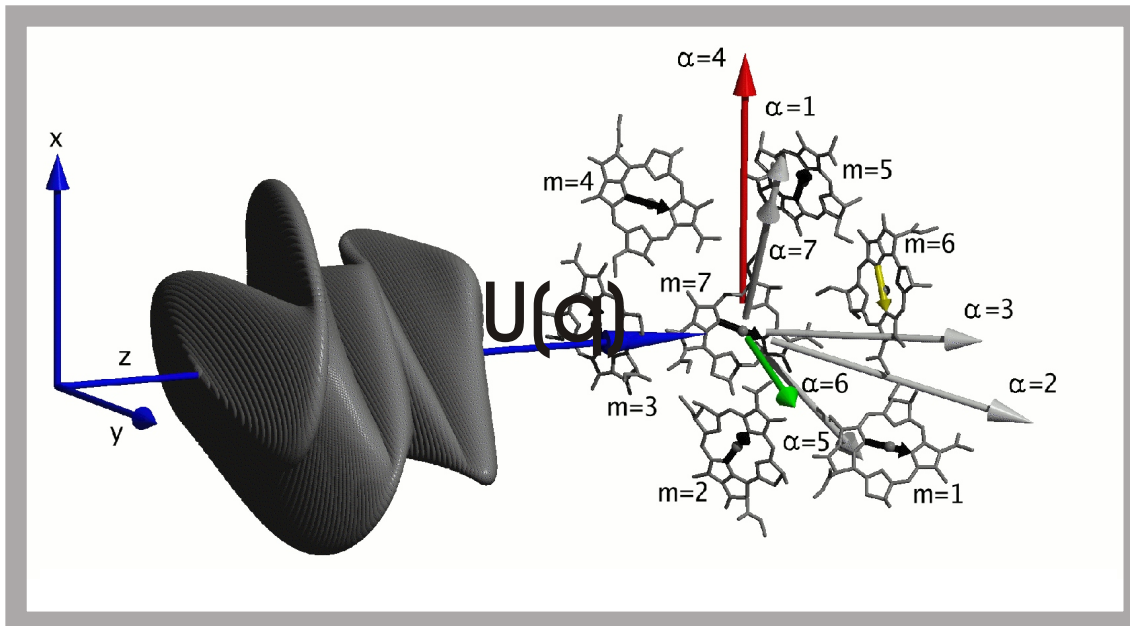
# laser pulse control of excitation energy transfer

$$|q, t\rangle = \sum_a c_a(t) |a, q\rangle$$



B. Brüggemann, T. Pullerits, and V. May  
 J. Photochem. Photobio. A 190, 372 (2007).

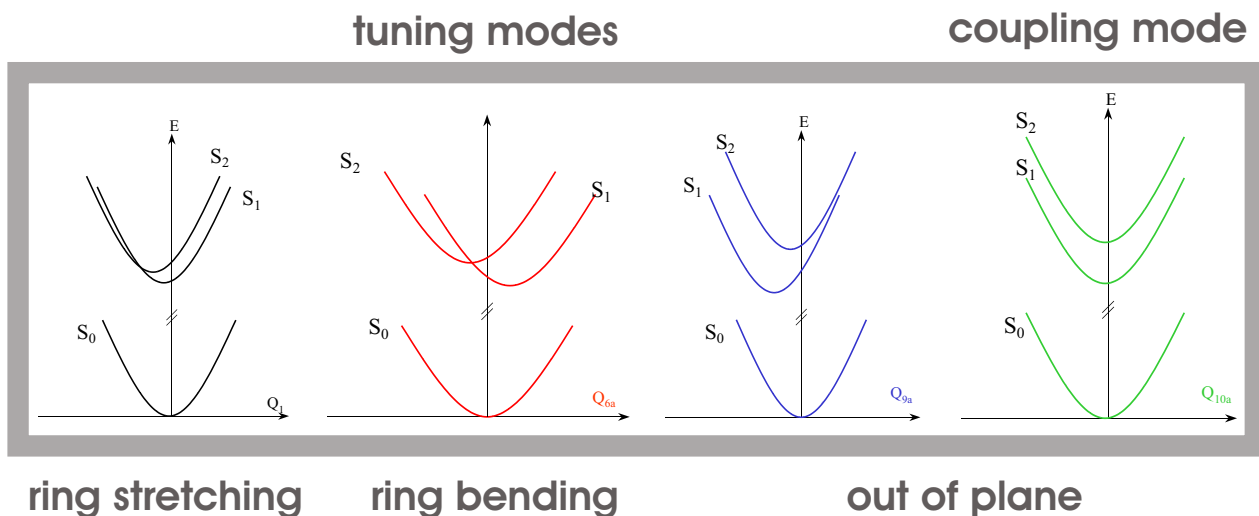
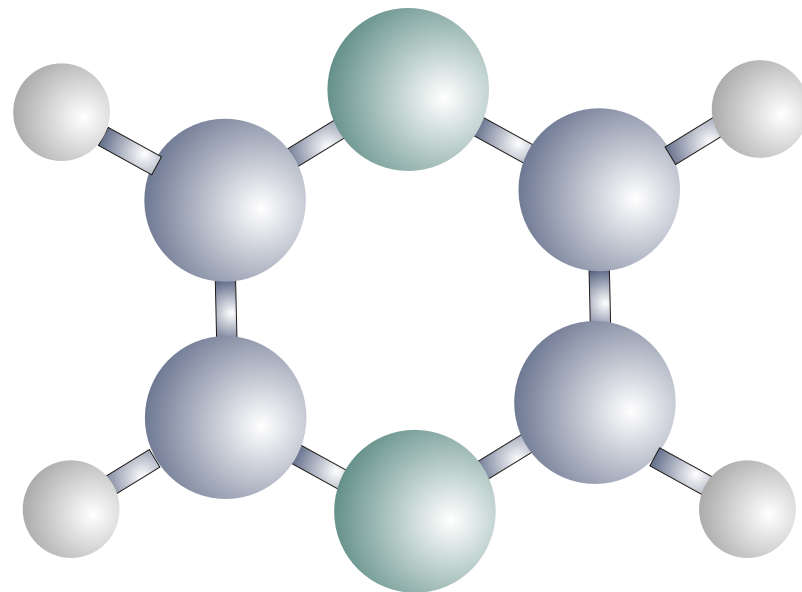
B. Brüggemann and V. May  
 in "Analysis and Control of Ultrafast Photoinduced  
 Reactions", O. Kühn and L. Wöste (eds.),  
 Springer Series in Chemical Physics Vol. 87  
 (Springer-Verlag, 2007), p. 774.



# Laser Pulse Control of Nonadiabatic Transitions



# 4-Mode Model of Pyrazine (vibronic coupling model)



**Multiconfiguration  
Time-Dependent  
Hartree Method**

$$\chi_a(Q_1, \dots, Q_N; t) = \sum_{\kappa_1=1}^{M_1} \cdots \sum_{\kappa_N=1}^{M_N} A_{\kappa_1 \dots \kappa_N}^{(a)}(t) \prod_{j=1}^N \zeta_{\kappa_j}^{(a)}(Q_j, t)$$

$$\mathcal{O}[\mathbf{E}_c] = \text{tr}_S \{ \hat{O} \hat{\rho}(t_f) \}$$

$$\mathcal{O}[\mathbf{E}_c] = \int_{t_0}^{\infty} dt_f \int dp \text{tr}_S \{ \hat{O}(t_f; p) \hat{\rho}(t_f; p) \}$$

optimization of  
an observable  
at a finite time  
or in a time  
and parameter  
space interval

**control functional  
to be optimized  
-> Optimal Control  
Theory**

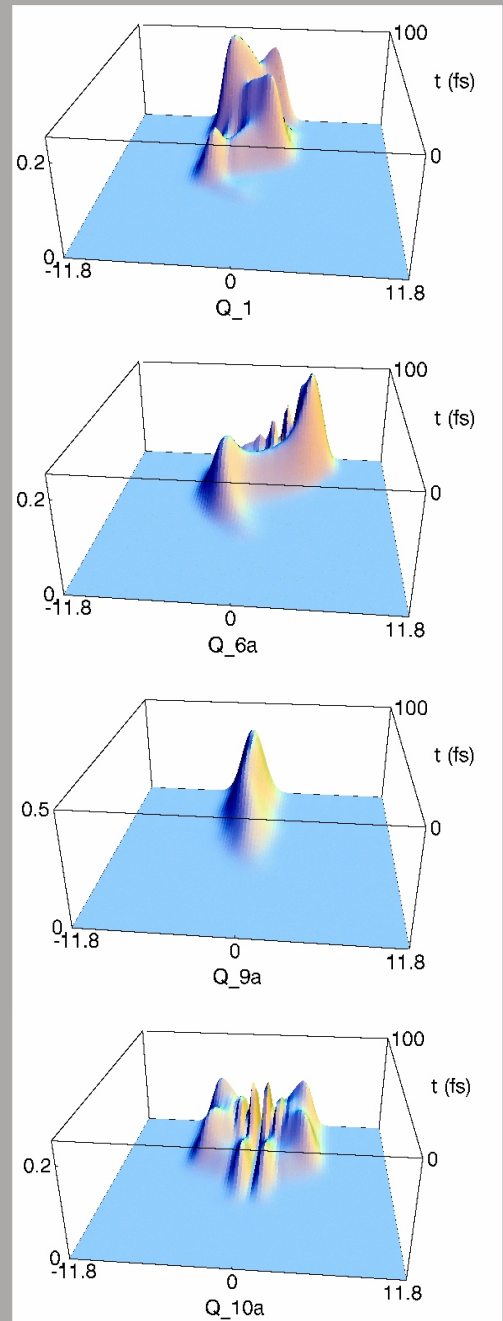
$$J[\mathbf{E}_c] = \mathcal{O}[\mathbf{E}_c] - \lambda \left( \frac{1}{2} \int_{t_0}^{t_f} dt \mathbf{E}_c^2(t) - I_0 \right)$$

**functional equation  
determining  
the optimal  
pulse**

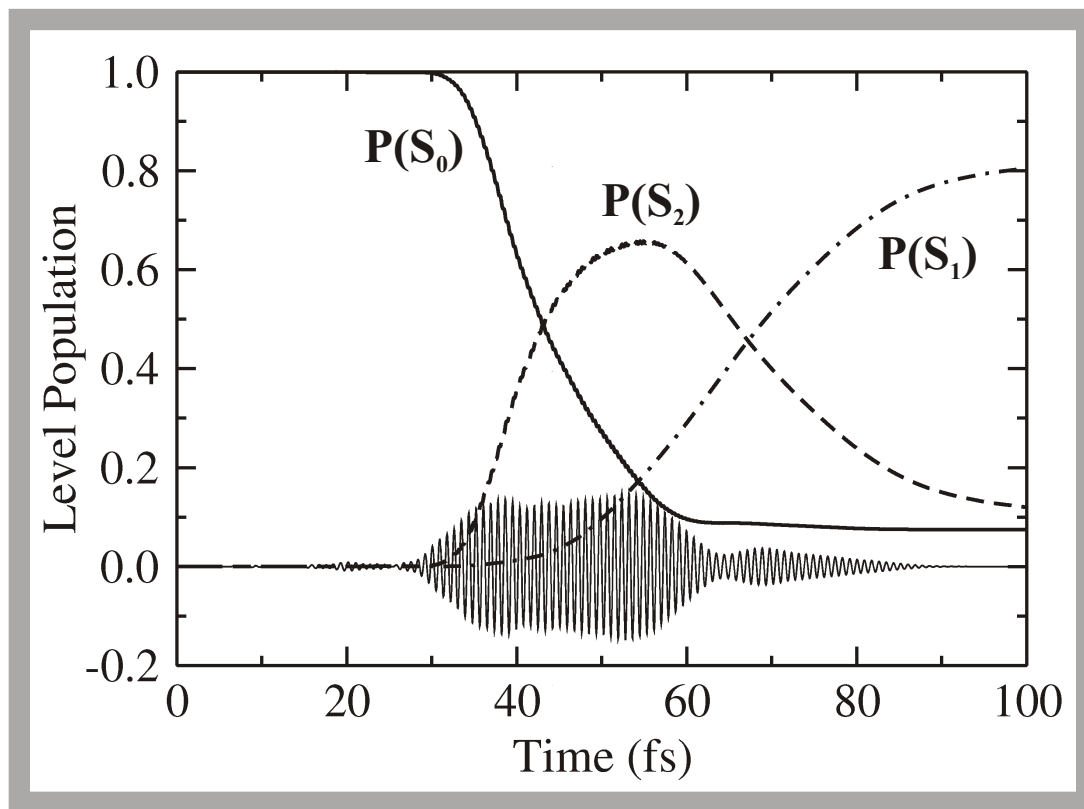
$$\mathbf{E}_c(t) = \frac{i}{\hbar \lambda} \int dp \text{tr}_S \{ \hat{O}(t; p) \mathcal{U}(t_f, t; p; \mathbf{E}_c) [\hat{\mu}, \hat{\rho}(t; p)] \}$$

L. Wang, H.-D. Meyer, and V. May:  
**Femtosecond Laser Pulse Control of Multidimensional Vibrational  
 Dynamics: Computational Studies on the Pyrazine Molecule**  
**J. Chem. Phys. 125, 014102 (2006).**

**Optimization of the overall  $S_1$ -population**



**Reduced  
 probability  
 distribution  
 of the  
 four modes**



$$P_{S_1}(Q_j, t) = \int dQ' |\chi_{S_1}(Q_1, Q_{6a}, Q_{9a}, Q_{10a}, t)|^2$$

# Heterogeneous Electron Transfer



**L. Wang, V. M., et al.:**

**Laser Pulse Control of Bridge Mediated Heterogeneous Electron Transfer**

Chem. Phys. (in press).

**Ultrafast Photoinduced Electron Transfer from Anchored Molecules into Semiconductors**

in "Analysis and Control of Ultrafast Photoinduced Reactions",

O. Kühn and L. Wöste (eds.), Springer Series in Chemical Physics Vol. 87

(Springer-Verlag, 2007), p. 437.

**Theory of Ultrafast Heterogeneous Electron Transfer:**

**Contributions of Direct Charge Transfer Excitations to the Absorbance**

J. Chem. Phys. 126, 134110 (2007).

**Theory of Ultrafast Heterogeneous Electron Transfer**

Molecular Simulation (special issue on electron transfer) 32, 765 (2006).

**Heterogeneous Electron Transfer Reactions:**

**Comparative Theoretical Studies in the Time and Frequency Domain**

J. Chem. Phys. 124, 014712 (2006).

**Absorption Spectra Related to Heterogeneous Electron Transfer Reactions:**

**The Perylene-TiO<sub>2</sub> System**

J. Phys. Chem. B 109, 9589 (2005).

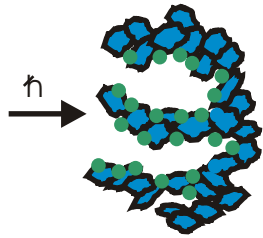
**Laser Pulse Control of Ultrafast Heterogeneous Electron Transfer: A Computational Study**

J. Chem. Phys. 121, 8039 (2004).

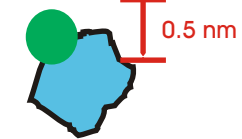
# Molecule Semiconductor-Surface System

## Perylene on $\text{TiO}_2$

$\text{TiO}_2$  nanoparticles

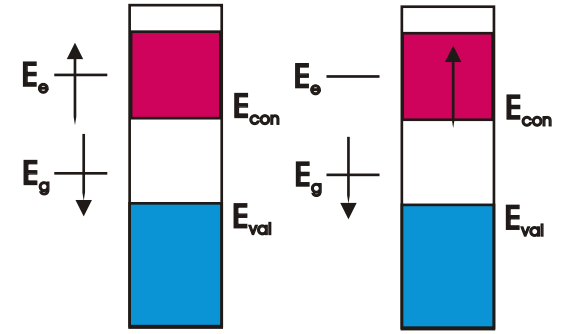
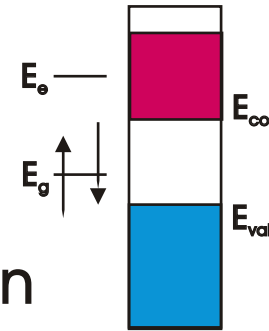
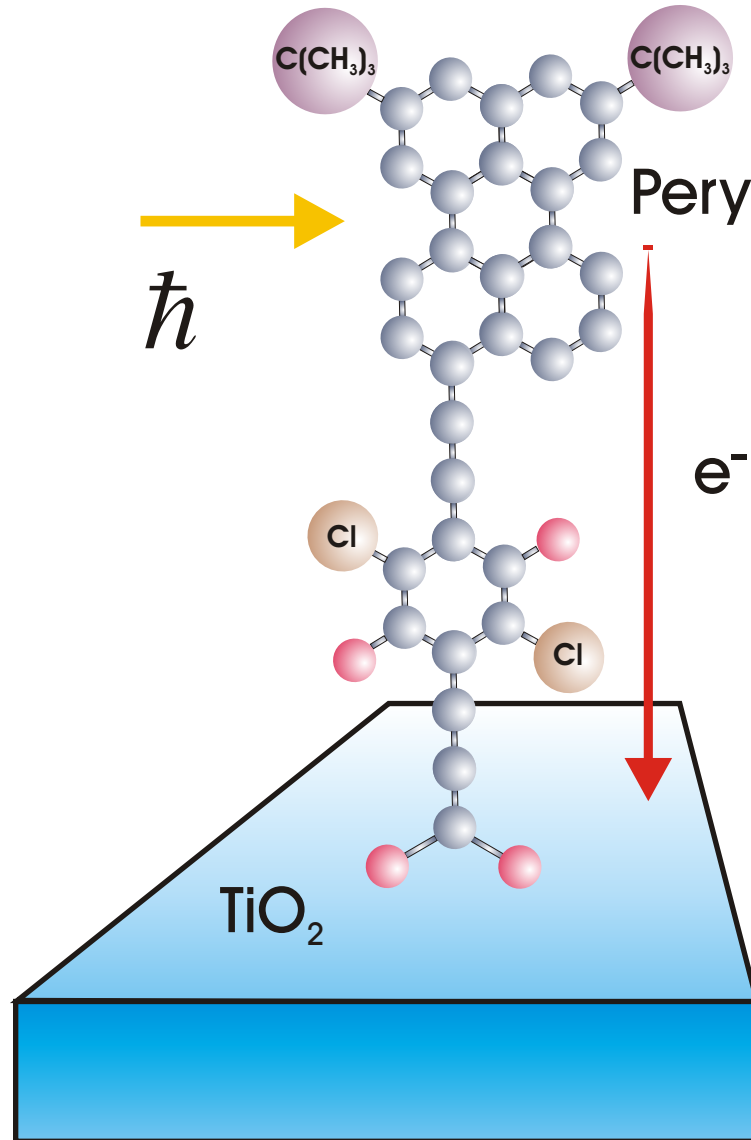


dye



$$\text{HET} = 10 \dots 57 \text{ fs}$$

$$\text{vib} = 1370 \text{ cm}^{-1}$$

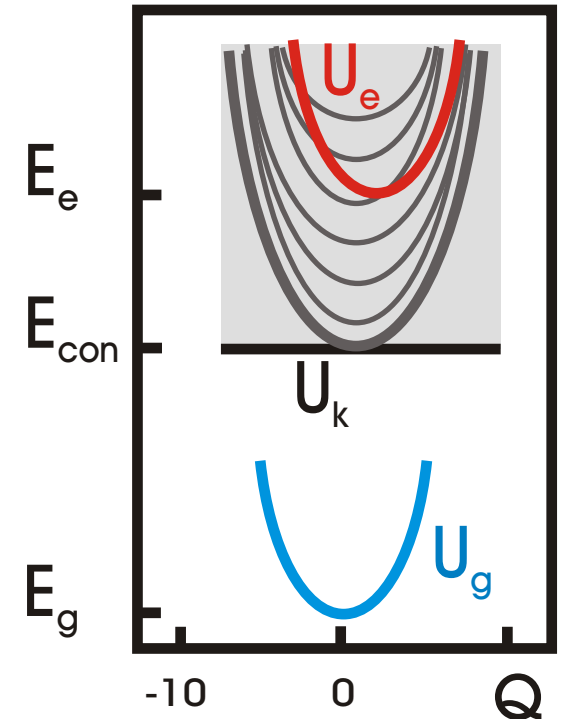


diabatic states

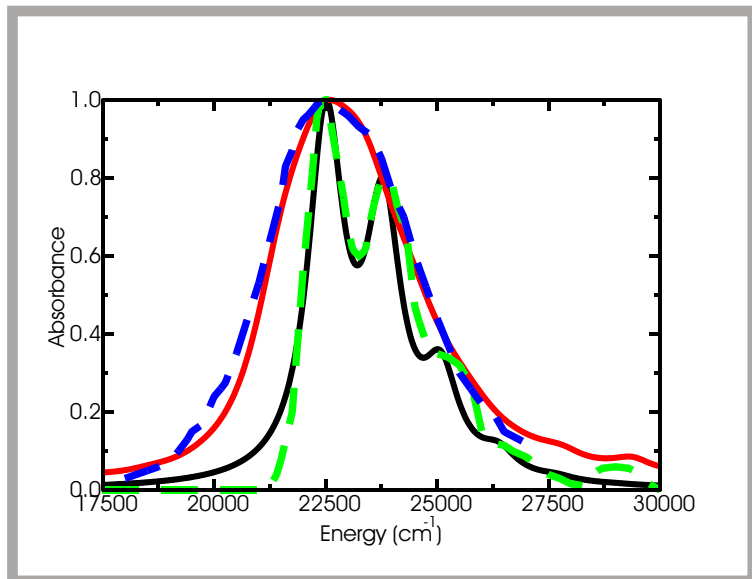
$|D\rangle |A\rangle$

$|D^*\rangle |A\rangle$

$|D^+\rangle |A^-\rangle$



# Linear Absorption of Perylene



broken lines:  
measured data

full lines:  
simulations

black and green:  
solvent case

blue and red:  
perylene on TiO<sub>2</sub>  
(DTB-Pe-COOH)

## Model Hamiltonian

$$H_{\text{mol-sem}} = \sum_{a=g,e,\mathbf{k}} (E_a + H_a) |\varphi_a\rangle \langle \varphi_a| + \sum_{\mathbf{k}} (V_{\mathbf{k}e} |\varphi_{\mathbf{k}}\rangle \langle \varphi_e| + V_{e\mathbf{k}} |\varphi_e\rangle \langle \varphi_{\mathbf{k}}|)$$

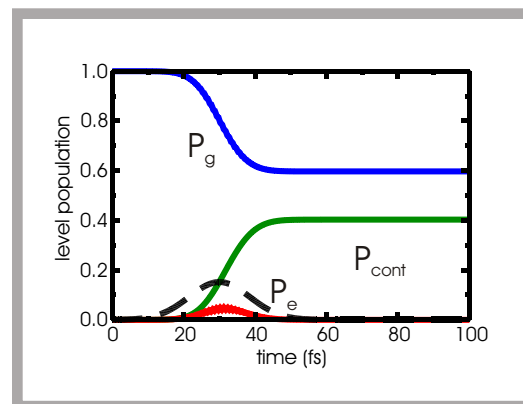
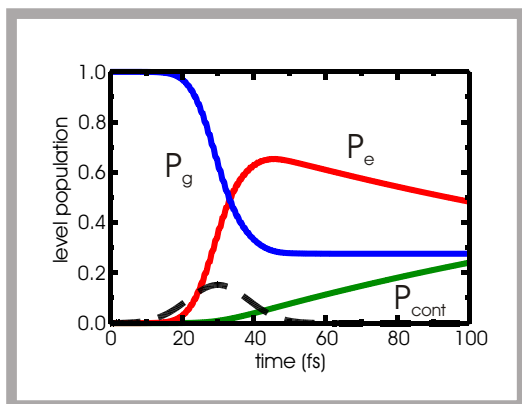
## DOS

$$\mathcal{N}(\Omega) = \sum_{\mathbf{k}} \delta(\Omega - \omega_{\mathbf{k}})$$

## Change of the Injection Time

$V = 0.02 \text{ eV}$

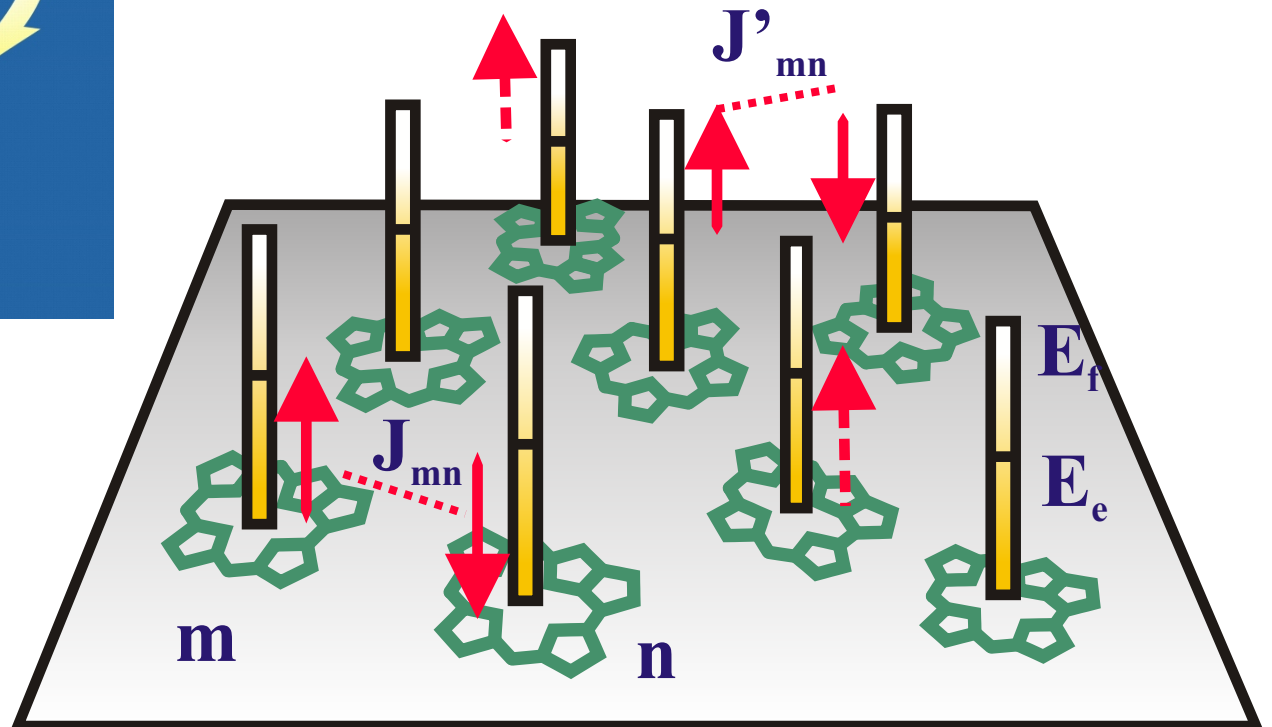
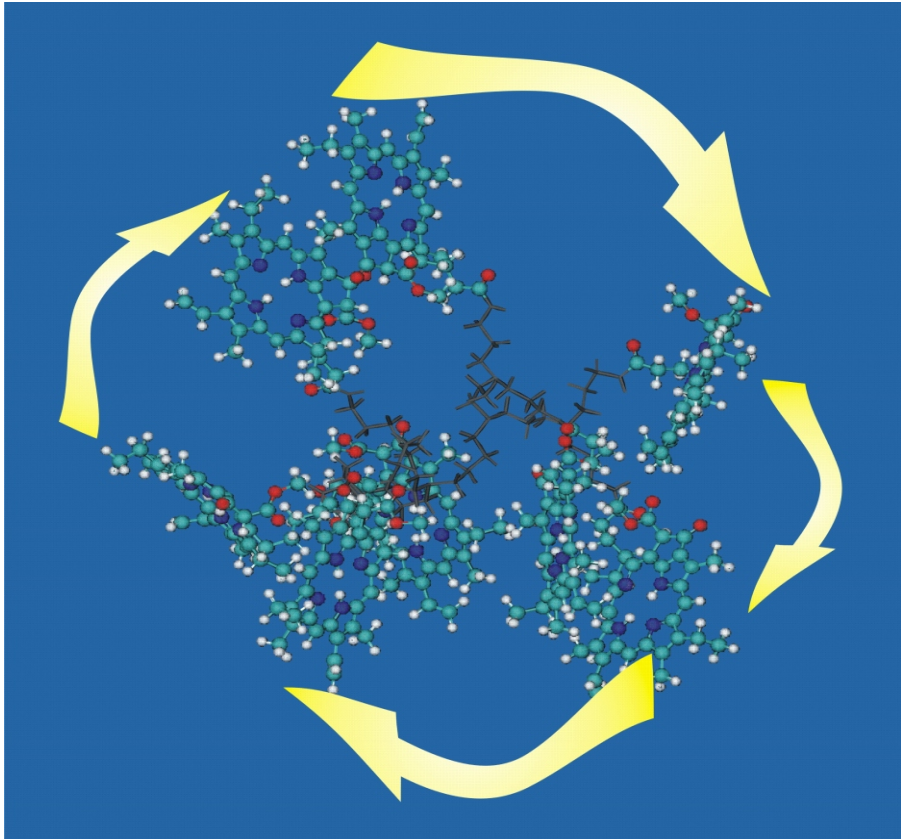
$V = 0.2 \text{ eV}$



## Basis Set Expansion of the Electron-Vibrational State Vector

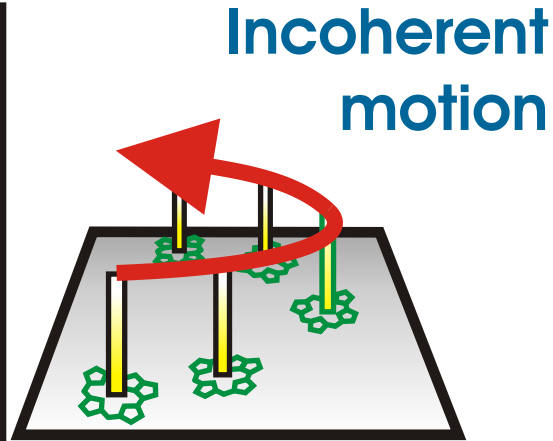
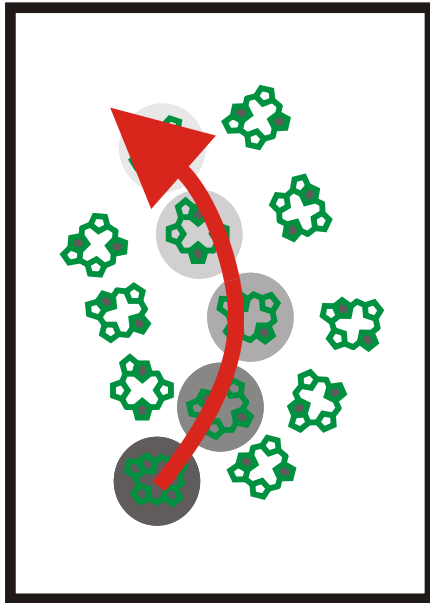
$$|\Psi(t)\rangle = \sum_{a=g,e,\mathbf{k}} \sum_M C_{aM}(t) |\chi_{aM}\rangle |\varphi_a\rangle$$

# Excitation Energy Transfer in Chromophore Complexes

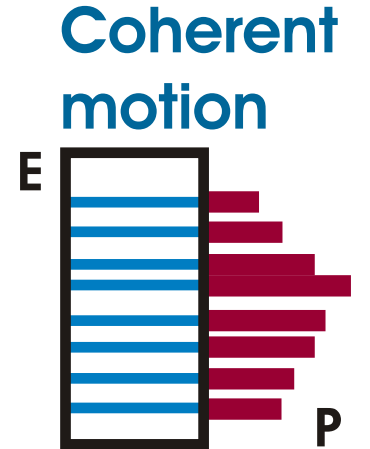
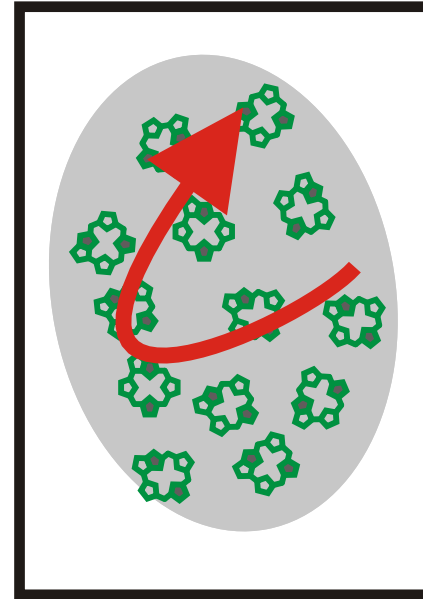




# Schemes of Excitation Energy Transfer



Incoherent motion



Coherent motion

$$|\phi_m\rangle = |\varphi_{me}\rangle \prod_{n \neq m} |\varphi_{ng}\rangle$$

site representation

$$H_{\text{ex}} = \sum_{mn} \left( \delta_{m,n} [T_{\text{muc}} + U_m(R)] + [1 - \delta_{m,n}] J_{mn}(R) \right) |\phi_m\rangle \langle \phi_n|$$

$$|\alpha\rangle = \sum_m C_\alpha(m) |\phi_m\rangle$$

exciton representation

$$H_{\text{ex}} = \sum_\alpha \left( \mathcal{E}_\alpha + \sum_\xi \hbar\omega_\xi C_\xi^+ C_\xi \right) |\alpha\rangle \langle \alpha| + \sum_{\alpha,\beta} \sum_\xi \hbar\omega_\xi g_{\alpha\beta}(\xi) \left( C_\xi + C_\xi^+ \right) |\alpha\rangle \langle \beta|$$

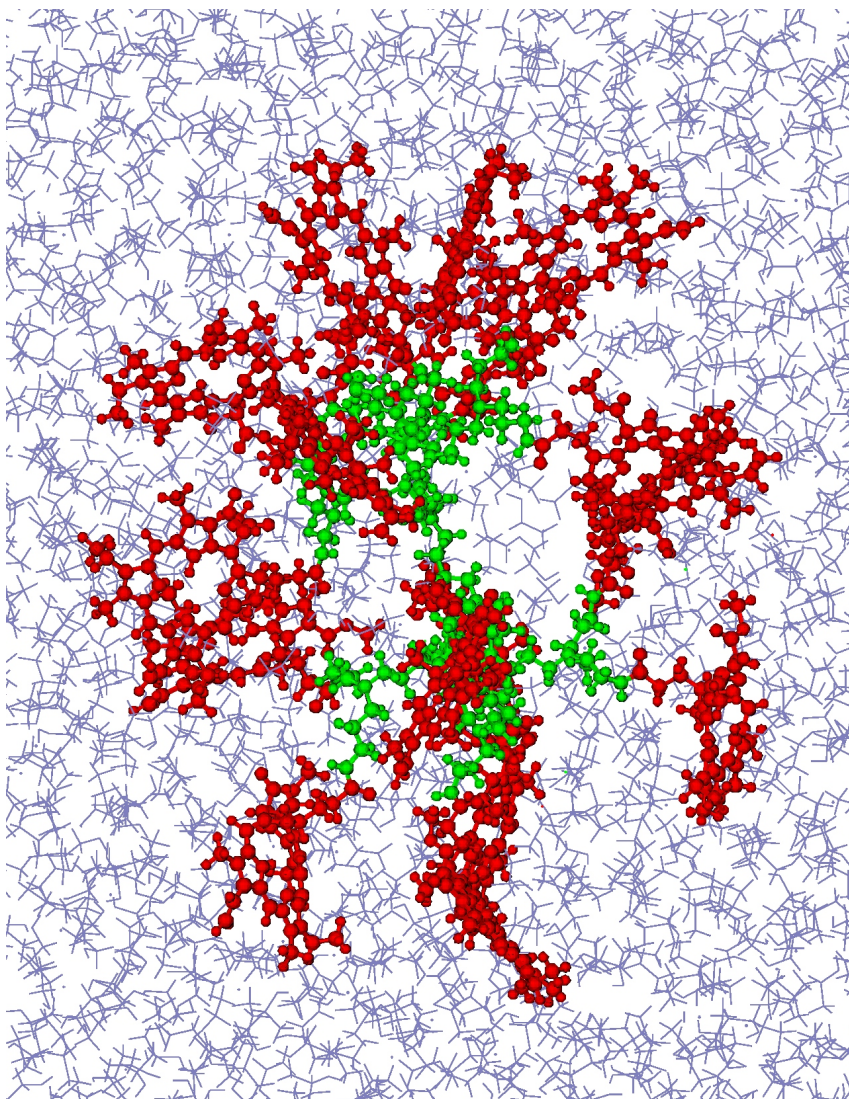
# Mixed Quantum Classical Description of Excitation Energy Transfer:

## Pheoporbide-a Complexes in Ethanol

V. H. Zhu, V. May, B. Röder, and Th. Renger,  
J. Chem. Phys. 128, 154905 (2008).

H. Zhu, V. May, and B. Röder,  
Chem. Phys. 351, 117 (2008).

H. Zhu and V. May,  
Springer Series in Chemical Physics  
(Springer-Verlag, 2009).

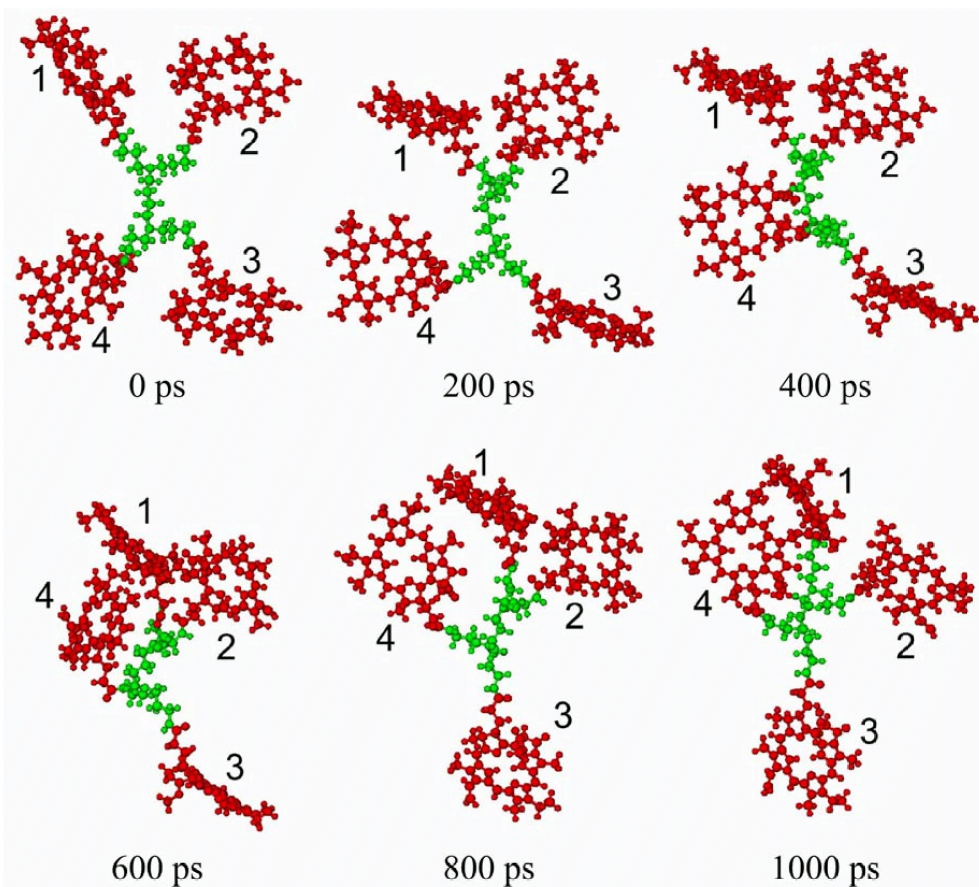


# Ehrenfest dynamics

$$i\hbar \frac{\partial}{\partial t} \Phi(r, R(t); t) = H_{\text{ex}}(R(t)) \Phi(r, R(t); t)$$

$$M_\nu \frac{\partial^2}{\partial t^2} \mathbf{R}_\nu(t) = -\nabla_\nu \langle \Phi(R(t); t) | H_{\text{ex}}(R(t)) | \Phi(R(t); t) \rangle$$

MD simulations  
of the solvent-  
solute system



-> exact account for exciton  
vibrational coupling

-> atomic resolution of  
vibrational dynamics

-> back reaction of the electron  
dynamics on the nuclear motion

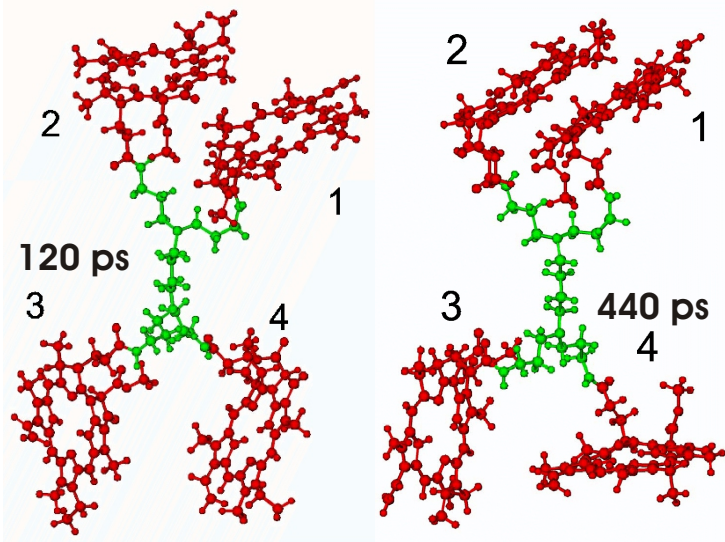
-> high-temperature limit

snapshots of  $P_4$  in ethanol along  
a 1 ns room-temperature MD run



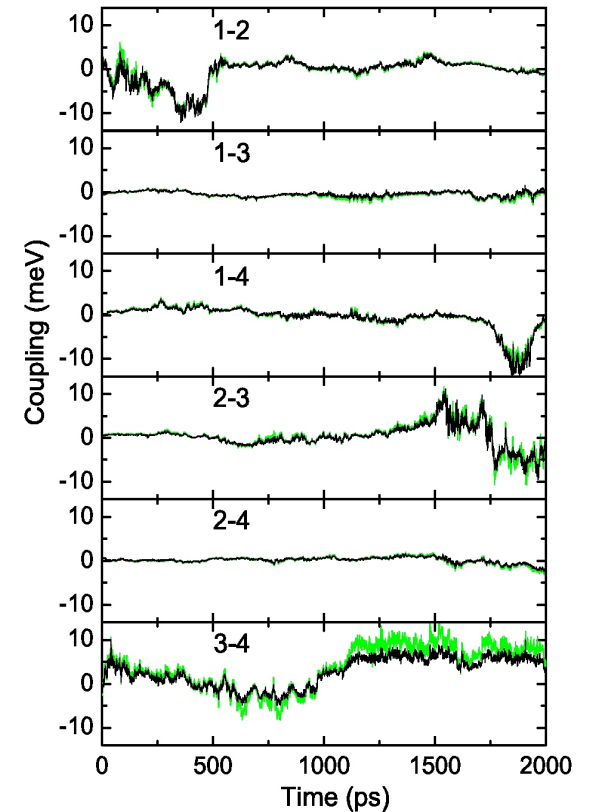
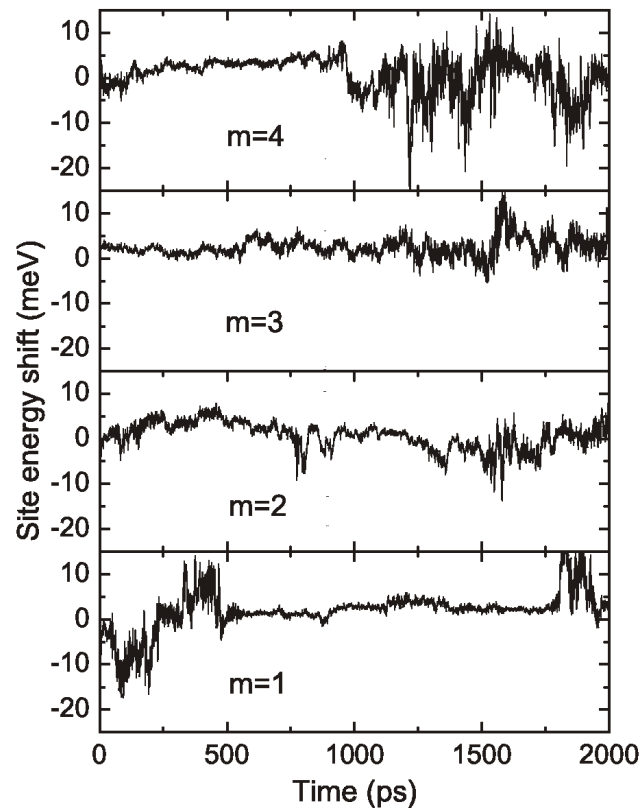
# single chromophore excitation energies and excitonic couplings

(coupling to solvent molecules  
has been neglected)



4 pheophorbide-a molecules  
covalently linked to a  
butanediamine dendrimer

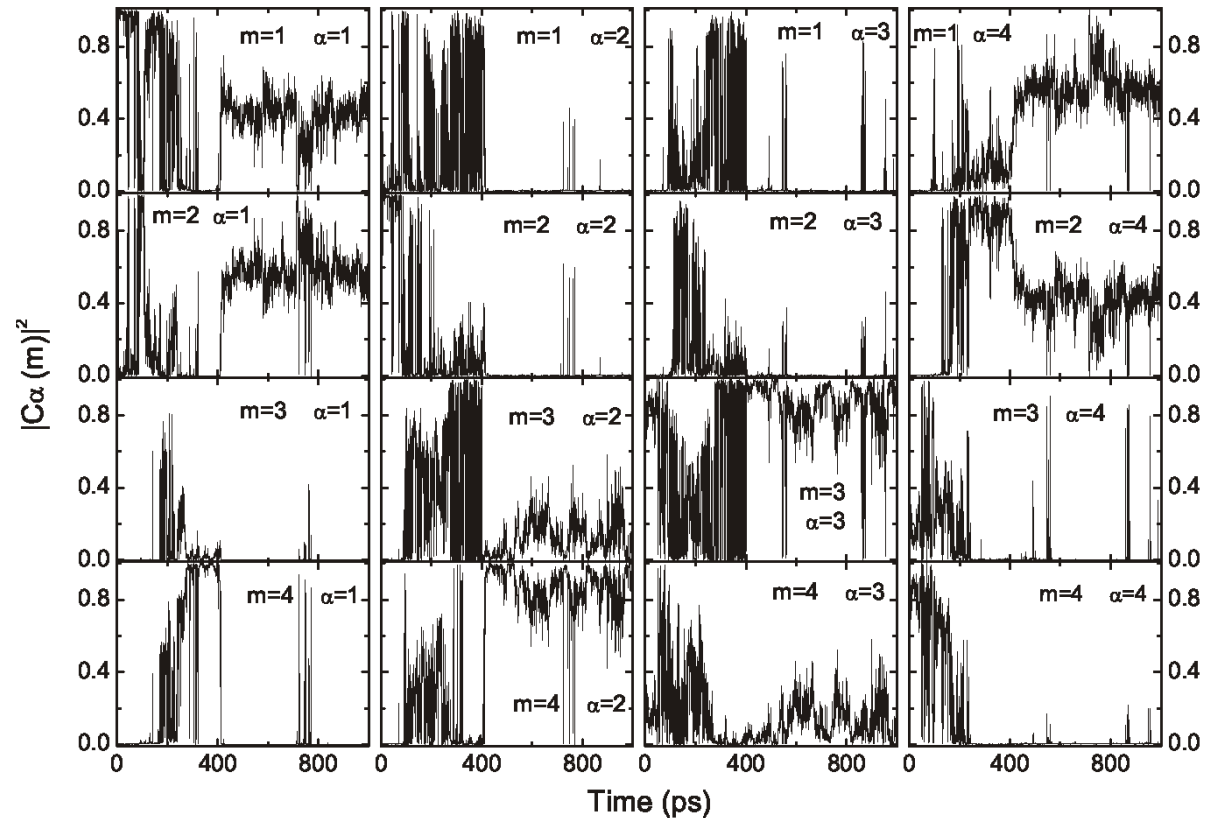
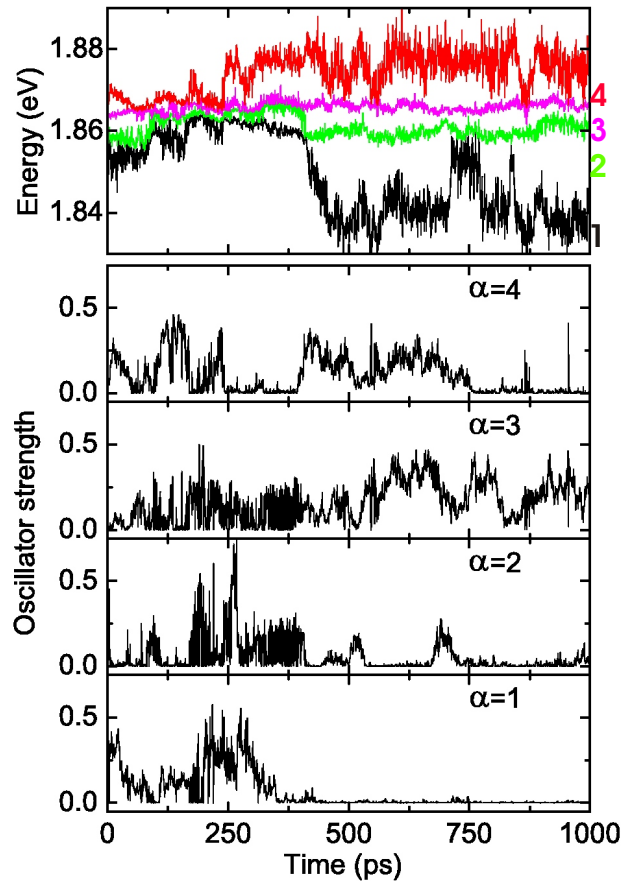
H. Zhu, V. May, B. Röder,  
M. El-Amine Madjet,  
and Th. Renger,  
Chem. Phys. Lett.  
444, 118 (2007).





# Adiabatic (instantaneous) excitons

energies, oscillator strengths, and expansion coefficients  
(coupling to solvent molecules has been neglected)

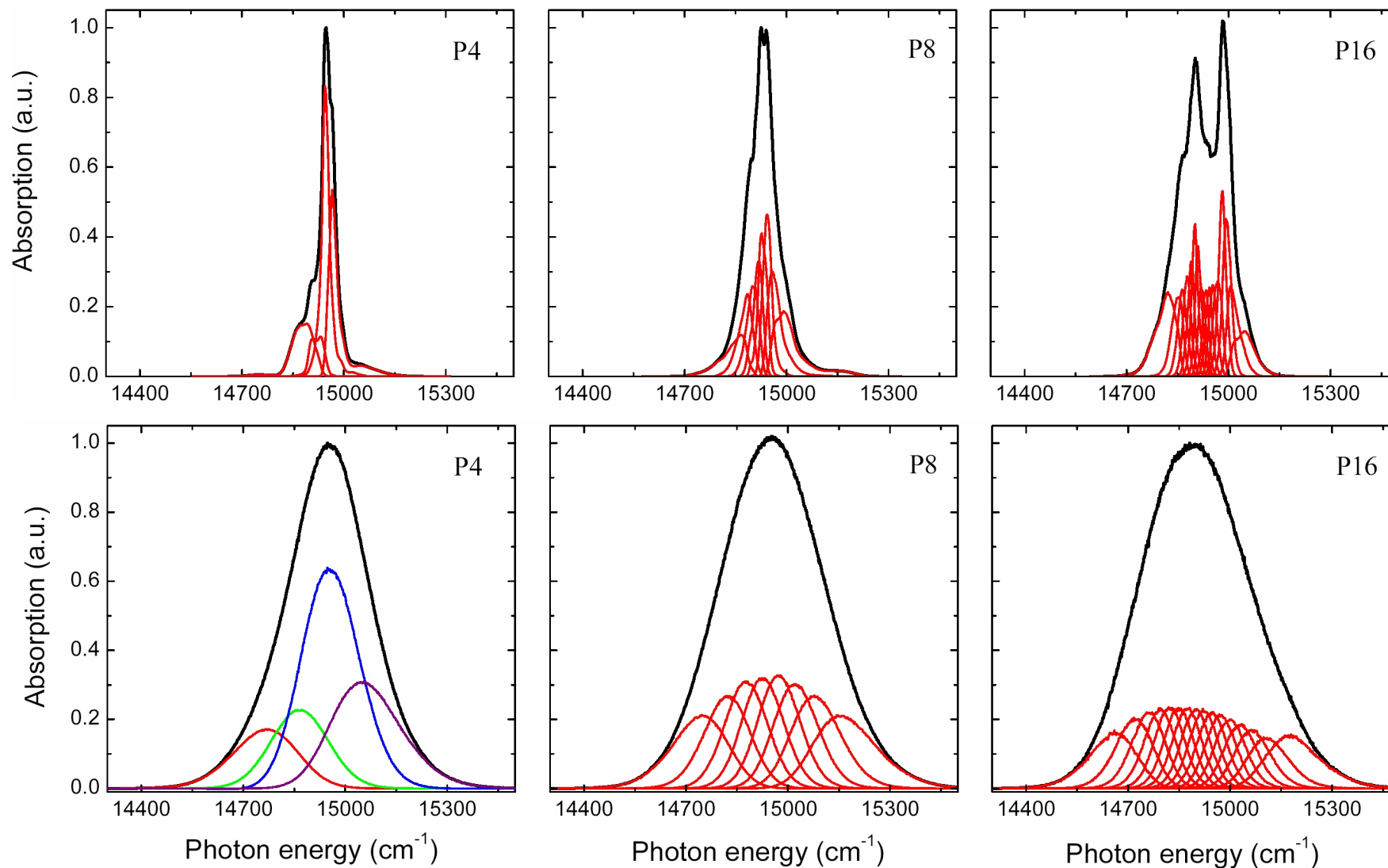


Adiabatic exciton energies and oscillator strengths (data have been computed every 0.5 ps within a single 1 ns MD run)

Square of adiabatic exciton expansion coefficients, taken at every 0.5 ps

# Linear Absorption Spectra

The modulation of the single chromophore excitation energy by the solvent molecules is **neglected**.

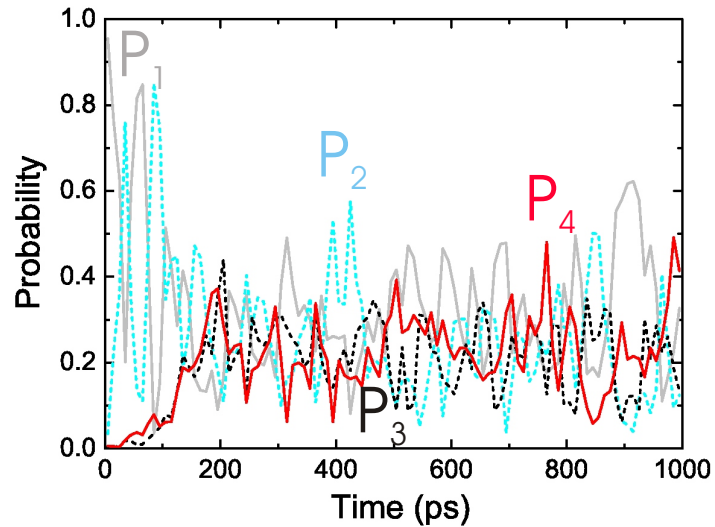


The modulation of the single chromophore excitation energy by the solvent molecules is **included**.

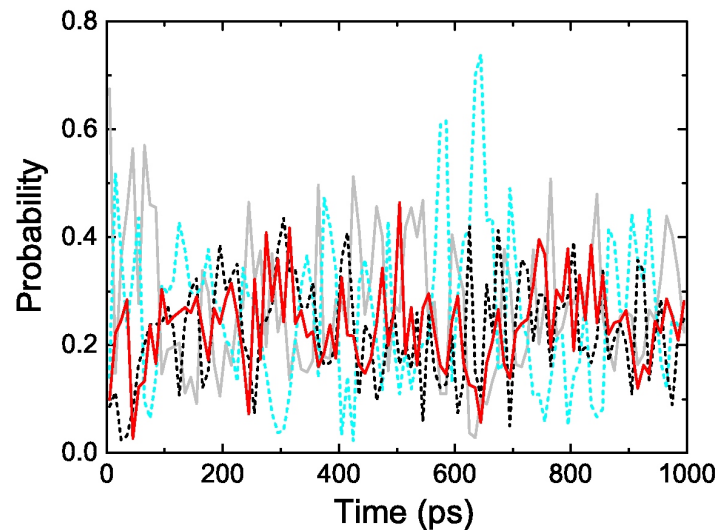
# Excitation Energy Transfer Dynamics

averaged with respect to a 10 ps time slice

$$P_m(t) = \langle |A_m(t)|^2 \rangle_{\text{ens}}$$

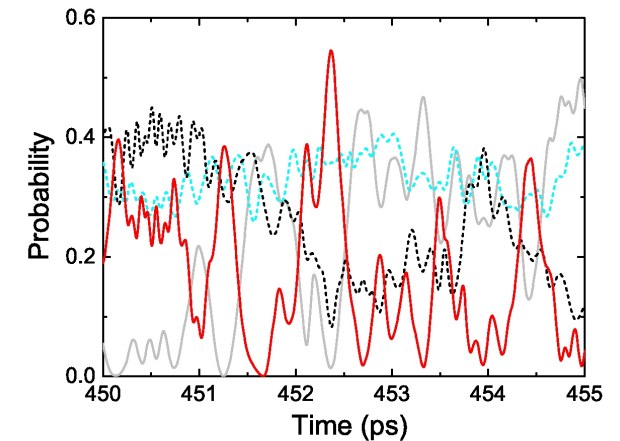
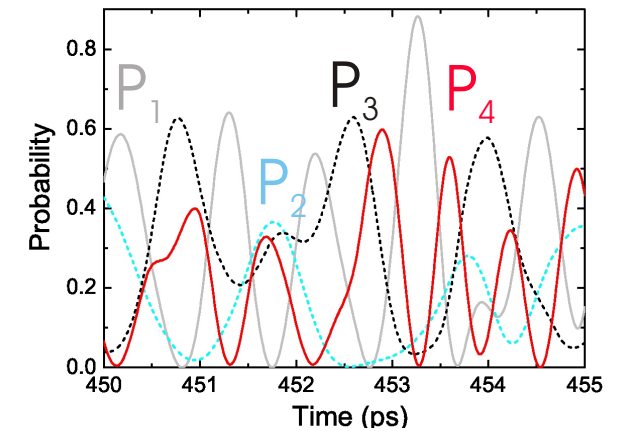


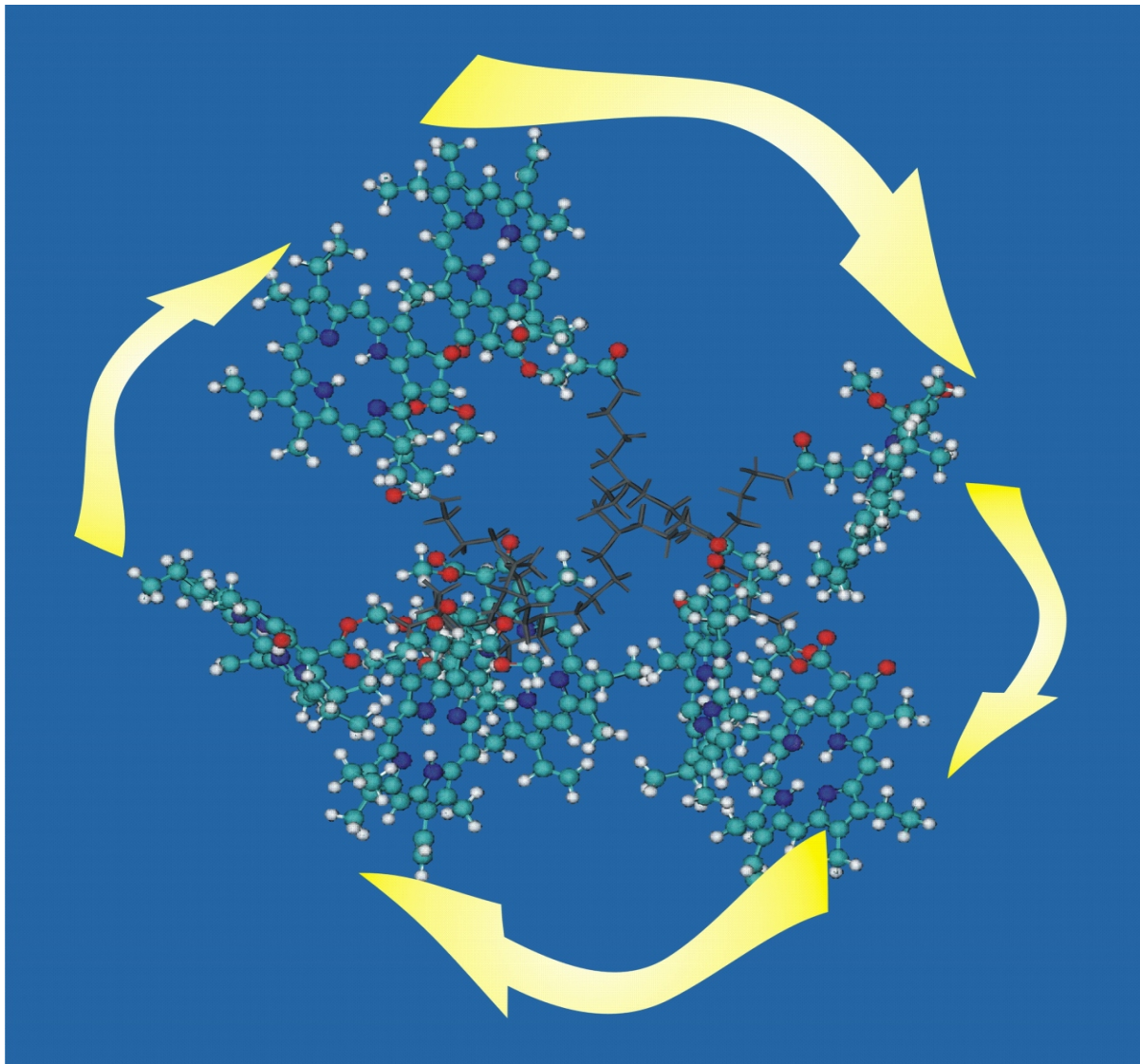
The modulation of the single chromophore excitation energy by the solvent molecules is neglected.



The modulation of the single chromophore excitation energy by the solvent molecules is included.

without time averaging

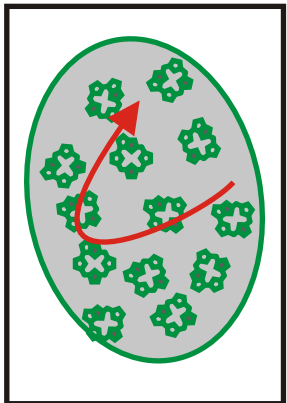
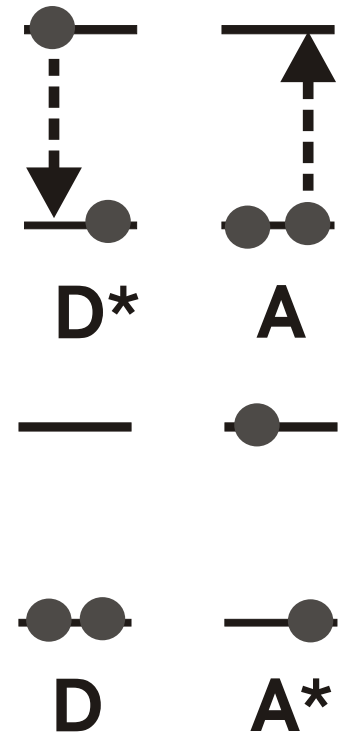
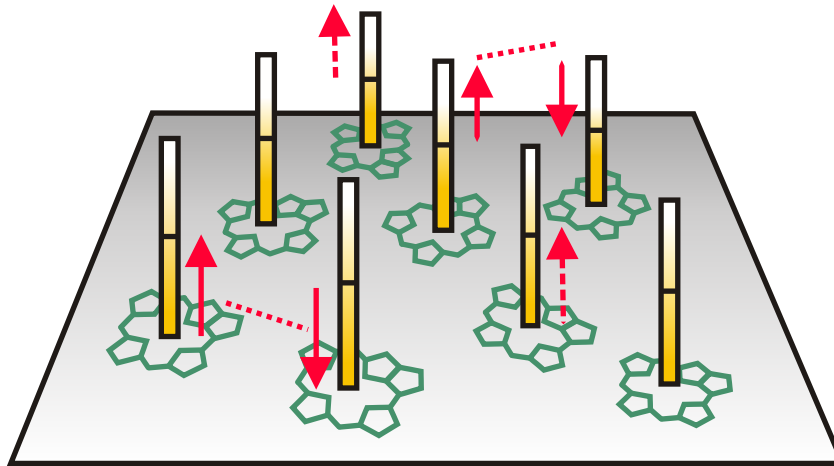
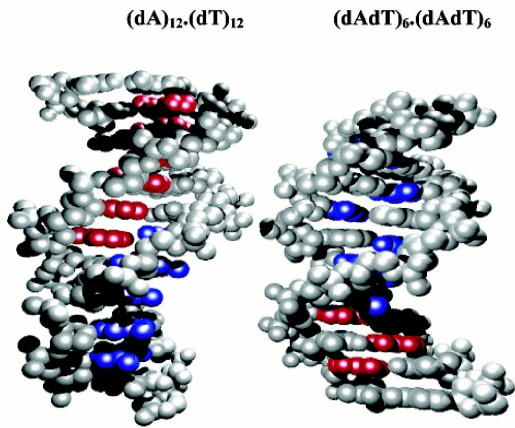




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Thanks  
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attention

